


# Search for $h_c \rightarrow \pi^+ \pi^- J/\psi$ via $\psi(3686) \rightarrow \pi^0 h_c$

M. Ablikim *et al.*\*  
(BESIII Collaboration)

 (Received 1 September 2024; accepted 13 November 2024; published 11 December 2024)

Using  $(2712.4 \pm 14.3) \times 10^6$   $\psi(3686)$  events collected with the BESIII detector operating at the BEPCII collider, we search for the hadronic transition  $h_c \rightarrow \pi^+ \pi^- J/\psi$  via  $\psi(3686) \rightarrow \pi^0 h_c$ . No significant signal is observed. We set the most stringent upper limits to date on the branching fractions  $\mathcal{B}(\psi(3686) \rightarrow \pi^0 h_c) \times \mathcal{B}(h_c \rightarrow \pi^+ \pi^- J/\psi)$  and  $\mathcal{B}(h_c \rightarrow \pi^+ \pi^- J/\psi)$  at the 90% confidence level, which are determined to be  $6.7 \times 10^{-7}$  and  $9.4 \times 10^{-4}$ , respectively.

DOI: [10.1103/PhysRevD.110.112010](https://doi.org/10.1103/PhysRevD.110.112010)

## I. INTRODUCTION

The study of charmonium decays is crucial to elucidate the mechanism of quantum chromodynamics (QCD), as these states lie in the transition region between nonperturbative and perturbative QCD. Although QCD has successfully explained many aspects of strong interactions, some known charmonium decay mechanisms remain challenging, as documented in Ref. [1].

Following identification of spin-singlet  $P$ -wave charmonium state  $h_c(^1P_1)$  in 2005 [2,3], extensive theoretical and experimental efforts have been made to understand its characteristics. The study of  $h_c$  remains difficult due to its relatively low branching fraction (BF), because its production through  $1^{--}$  charmonia is suppressed [4].

The first evidence for the  $h_c$  state was reported by E835 at Fermilab in the  $p\bar{p} \rightarrow h_c \rightarrow \gamma\eta_c$  process [5]. Subsequently, the CLEO experiment presented the first observation of the  $h_c$  in a study of the cascade decay  $\psi(3686) \rightarrow \pi^0 h_c$ ,  $h_c \rightarrow \gamma\eta_c$  [6], measured its mass [7], and provided evidence for its multipion decay modes [8]. The BESIII collaboration made the first measurement of the absolute BFs,  $\mathcal{B}(\psi(3686) \rightarrow \pi^0 h_c)$  and  $\mathcal{B}(h_c \rightarrow \gamma\eta_c)$  [9], which were later confirmed by CLEO [10]. With a larger  $\psi(3686)$  data sample, recent experimental measurements give  $\mathcal{B}(\psi(3686) \rightarrow \pi^0 h_c) = (7.32 \pm 0.34 \pm 0.41) \times 10^{-4}$  and  $\mathcal{B}(h_c \rightarrow \gamma\eta_c) = (57.66_{-3.50}^{+3.62} \pm 0.58)\%$  [11]. These indicate that the sum of the  $h_c$  hadronic decay modes is comparable to its radiative transition rate.

The hadronic transitions of  $h_c$  provide a valuable opportunity to investigate the spin-spin interaction between heavy quarks [12]. The Feynman diagram of the hadronic transition  $h_c \rightarrow \pi^+ \pi^- J/\psi$  is depicted in Fig. 1. According to theoretical predictions based on a QCD multipole expansion, the BF of  $h_c \rightarrow \pi\pi J/\psi$  (including charged and neutral modes) is predicted to be 2% [13]. However, when nonlocality in time is neglected, the predicted BF decreases significantly to 0.05% [14]. Additionally, Ref. [15] suggests that the BF for  $h_c \rightarrow \pi^+ \pi^- J/\psi$  is approximately 40 times smaller than that for  $h_c \rightarrow \pi^0 J/\psi$ .

In 2018, the BESIII collaboration searched for the hadronic transition of  $h_c \rightarrow \pi^+ \pi^- J/\psi$  using a dataset of  $(448.1 \pm 0.8)$  million  $\psi(3686)$  events [16]. The upper limit on the product of BFs,  $\mathcal{B}(\psi(3686) \rightarrow \pi^0 h_c) \times \mathcal{B}(h_c \rightarrow \pi^+ \pi^- J/\psi)$ , was determined to be  $2.0 \times 10^{-6}$  at the 90% confidence level (CL) [17], which is in better agreement with the theoretical prediction presented in Ref. [14]. Four years later, the BESIII Collaboration reported the upper limit on  $\mathcal{B}(h_c \rightarrow \pi^0 J/\psi)$  which was determined to be  $4.7 \times 10^{-4}$  at the 90% CL, utilizing  $11 \text{ fb}^{-1}$  of  $e^+e^-$  collision data taken at center-of-mass energies between 4.189 and 4.437 GeV [18]. According to

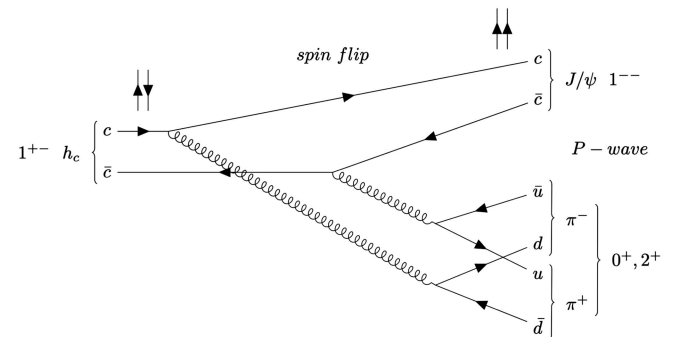


FIG. 1. The Feynman diagram for the spin flip hadronic transition  $h_c \rightarrow \pi^+ \pi^- J/\psi$ .

\*Full author list given at the end of the article.

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Ref. [15], this result suggests that  $\mathcal{B}(h_c \rightarrow \pi^+\pi^-J/\psi)$  could be smaller than  $1.2 \times 10^{-5}$ .

In this paper, based on  $(2712.4 \pm 14.3) \times 10^6$   $\psi(3686)$  events [16,19], we present an updated analysis of a search for the hadronic transition  $h_c \rightarrow \pi^+\pi^-J/\psi$ .

## II. BESIII DETECTOR AND MONTE CARLO SIMULATION

The BESIII detector [20] records symmetric  $e^+e^-$  collisions provided by the BEPCII storage ring [21] in the center-of-mass energy range from 1.84 to 4.95 GeV, with a peak luminosity of  $1.1 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$  achieved at  $\sqrt{s} = 3.773$  GeV. BESIII has collected large data samples in this energy region [22–24]. The cylindrical core of the BESIII detector covers 93% of the full solid angle and consists of a helium-based multilayer drift chamber (MDC), a time-of-flight system (TOF), and a CsI(Tl) electromagnetic calorimeter (EMC), which are all enclosed in a superconducting solenoidal magnet providing a 1.0 T magnetic field. The solenoid is supported by an octagonal flux-return yoke with modules of resistive plate muon counters (MUC) interleaved with steel. The charged-particle momentum resolution at 1 GeV/ $c$  is 0.5%, and the  $dE/dx$  resolution is 6% for the electrons from Bhabha scattering. The EMC measures photon energy with a resolution of 2.5% (5%) at 1 GeV in the barrel (end-cap) region. The time resolution of the plastic scintillator TOF barrel part is 68 ps, while that of the end-cap part is 110 ps. The end cap TOF system was upgraded in 2015 using multigap resistive plate chamber technology, providing a time resolution of 60 ps, which benefits  $\sim 83\%$  of the data used in this analysis [25–27].

Monte Carlo (MC) simulated data samples produced with GEANT4-based [28] software, which includes the geometric description of the BESIII detector and the detector response, are used to optimize the event selection criteria and estimate the signal efficiency and level of background. The simulation models the beam-energy spread and initial-state radiation in the  $e^+e^-$  annihilation using the generator KKMC [29,30]. The inclusive MC sample includes the production of the  $\psi(3686)$  resonance, the initial-state radiation production of the  $J/\psi$  meson, and the continuum processes incorporated in KKMC. All particle decays are modeled with EVTGEN [31,32] using BFs either taken from the Particle Data Group (PDG) [4], when available, or otherwise estimated with LUNDCHARM [33,34]. Final-state radiation from charged final-state particles is incorporated using PHOTOS [35].

Corresponding to the total number of  $\psi(3686)$  events collected in different years, 2,712,400 signal MC events are generated with  $\psi(3686) \rightarrow \pi^0 h_c$  and  $J/\psi \rightarrow e^+e^-/\mu^+\mu^-$  modeled by PARTWAVE and PHOTOS VLL simulations [31,32], respectively. Additionally,  $\pi^0 \rightarrow \gamma\gamma$  and  $h_c \rightarrow \pi^+\pi^-J/\psi$  are modeled with a phase space (PHSP) model.

## III. EVENT SELECTION

The final-state particles in this analysis include  $\pi^+\pi^-\gamma\gamma\mu^+\mu^-$  and  $\pi^+\pi^-\gamma\gamma e^+e^-$ . Charged tracks detected in the MDC are required to be within a polar angle ( $\theta$ ) range of  $|\cos\theta| < 0.93$ , where  $\theta$  is defined with respect to the  $z$ -axis, which is the symmetry axis of the MDC. For charged tracks, the distance of closest approach to the interaction point (IP) must be less than 10 cm along the  $z$ -axis,  $|V_z|$ , and less than 1 cm in the transverse plane,  $|V_{xy}|$ .

Photon candidates are identified using isolated showers in the EMC. The deposited energy of each shower must be more than 25 MeV in the barrel region ( $|\cos\theta| < 0.80$ ) and more than 50 MeV in the end-cap region ( $0.86 < |\cos\theta| < 0.92$ ). To exclude showers that originate from charged tracks, the angle subtended by the EMC shower and the position of the closest charged track at the EMC must be greater than 10 degrees as measured from the IP. To suppress electronic noise and showers unrelated to the event, the difference between the EMC time and the event start time is required to be within  $[0, 700]$  ns.

The number of good charged tracks is required to be four with zero net charge. The three-momenta in the laboratory frame is used to separate leptons and pions. Charged tracks with momentum below 1 GeV/ $c$  are assumed to be pions, while those with momentum above 1 GeV/ $c$  are taken as leptons. A pair of pions with opposite charge and a pair of leptons with the same flavor and opposite charge are required. Muons and electrons are separated based on their energy deposits in the EMC. Electrons and positrons must have energy deposits greater than 1.0 GeV, while muons have energy deposits less than 0.4 GeV.

The  $J/\psi$  candidates are reconstructed from  $e^+e^-$  and  $\mu^+\mu^-$  pairs with invariant mass in the  $J/\psi$  mass region, defined as  $3.085 < M(l^+l^-) < 3.108$  GeV/ $c^2$ , ( $l \equiv e, \mu$ ), which is about three times the standard deviation obtained from the fit to the distribution of the  $l^+l^-$  invariant mass  $M(l^+l^-)$  of data.

To suppress background, a five-constraint (5C) kinematic fit is performed, constraining the four-momentum of the final state particles to that of the initial system and the invariant mass of the  $\gamma\gamma$  pair to the  $\pi^0$  mass [4]. The four-momenta from the kinematic fit are used in the following analysis.

To suppress background from the decay  $\psi(3686) \rightarrow \eta J/\psi, \eta \rightarrow \pi^+\pi^-\pi^0$  and other background decays to different final states, we optimize two selection criteria, which are the requirements on  $\chi_{5C}^2$  and on the  $\pi^+\pi^-\pi^0$  invariant mass,  $M_{\pi^+\pi^-\pi^0}$ , by maximizing a figure-of-merit given by  $\epsilon_{\text{sig}}/(\alpha/2 + \sqrt{B})$ . Here the signal efficiency ( $\epsilon_{\text{sig}}$ ) is determined with the signal MC sample, the background yield ( $B$ ) is estimated using the inclusive MC sample, and  $\alpha$  is the significance level, which is set to be 3.0. Based on the optimization, the optimal requirements of  $\chi_{5C}^2 < 15$  and  $|M_{\pi^+\pi^-\pi^0} - M_\eta| > 24.5$  MeV/ $c^2$  are applied, where  $M_\eta$  is

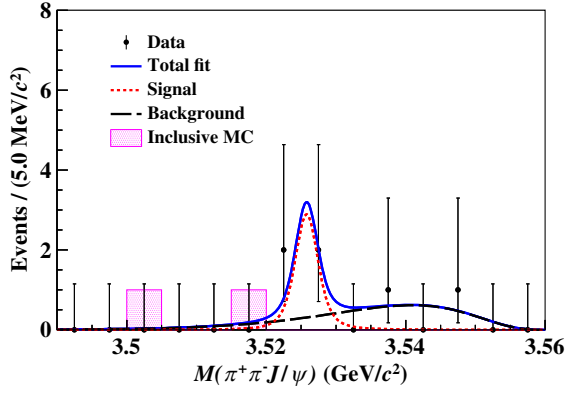


FIG. 2. The fit to the  $M(\pi^+\pi^-J/\psi)$  distribution. The points with errors bar are data, the blue solid curve is the fit result, the black solid dashed line is the background, the red dotted curve is the signal and the purple bars are the remaining inclusive MC events.

the  $\eta$  mass [4]. Additionally, a requirement of  $M(\pi^+\pi^-) > 0.3 \text{ GeV}/c^2$  has been applied to reduce the background from the decay  $\psi(3686) \rightarrow \pi^0\pi^0J/\psi$  with  $\gamma$  converting into an  $e^+e^-$  pair in the beam pipe or inner wall of the MDC and the  $e^+e^-$  pair is misidentified as  $\pi^+\pi^-$  pair. After applying the above selection criteria, only two background events from  $\psi(3686) \rightarrow \eta J/\psi, \eta \rightarrow \pi^+\pi^-\pi^0$  survive, which are shown as the purple bars in Fig. 2.

#### IV. SIGNAL YIELDS

To determine the signal yield, we perform an unbinned likelihood fit to the  $M(\pi^+\pi^-J/\psi)$  distribution of the accepted candidates, as shown in Fig. 2. The  $h_c$  signal is described using the shape obtained from signal MC events, while the combinatorial background shape is described by an ARGUS function [36]. The signal yield determined from the fit is  $N_{\text{sig}}^{\text{obs}} = 2.7 \pm 2.1$ . The statistical significance of the  $h_c$  signal is  $1.6\sigma$ , by comparing the log-likelihood values of the fits with and without signal component ( $\Delta \ln L = 1.26$ ) and taking the change in the number of degrees of freedom into account.

Since no significant signal of  $\psi(3686) \rightarrow \pi^0 h_c, h_c \rightarrow \pi^+\pi^-J/\psi$  is observed, the upper limit on the product BFs is calculated as

$$[\mathcal{B}(\psi(3686) \rightarrow \pi^0 h_c) \times \mathcal{B}(h_c \rightarrow \pi^+\pi^-J/\psi)]_{\text{upper}} = \frac{N_{\text{sig}}^{\text{up}}}{N_{\psi(3686)} \times \epsilon_{\text{sig}} \times \mathcal{B}(J/\psi \rightarrow l^+l^-) \times \mathcal{B}(\pi^0 \rightarrow \gamma\gamma)}. \quad (1)$$

Here,  $N_{\psi(3686)}$  is the number of  $\psi(3686)$  events and  $N_{\text{sig}}^{\text{up}}$  is the upper limit of  $h_c$  signal events obtained from a Bayesian method [37] with a prior density  $p$ , where  $p = 0$  for  $N_{\text{sig}} < 0$ , and  $p = 1$  for  $N_{\text{sig}} \geq 0$ . The detection efficiency of the signal mode is  $\epsilon_{\text{sig}} = 3.74\%$ . The BFs of the

intermediate states,  $\mathcal{B}(\pi^0 \rightarrow \gamma\gamma)$  and  $\mathcal{B}(J/\psi \rightarrow l^+l^-)$ , are taken from the PDG [4]. The upper limit on  $\mathcal{B}(\psi(3686) \rightarrow \pi^0 h_c) \times \mathcal{B}(h_c \rightarrow \pi^+\pi^-J/\psi)$  is determined to be  $6.7 \times 10^{-7}$  incorporating the systematic uncertainties that will be addressed in Sec. V.

#### V. SYSTEMATIC UNCERTAINTIES

The systematic uncertainty for the upper limit of the BF includes multiplicative and additive sources. The multiplicative systematic uncertainties are from the number of  $\psi(3686)$  events, tracking, photon detection, kinematic fit, quoted BFs, mass windows, and the signal model. Details of the systematic uncertainties are discussed below:

- (i) Number of  $\psi(3686)$  events: The uncertainty on the number of  $\psi(3686)$  events, determined with inclusive hadronic  $\psi(3686)$  decays, is 0.5% [16,19].
- (ii) Tracking: The uncertainties of the tracking efficiencies for charged pions and leptons are estimated with a control sample of  $\psi(3686) \rightarrow \pi^+\pi^-J/\psi, J/\psi \rightarrow e^+e^-(\mu^+\mu^-)$ . The MC simulation is re-weighted in two-dimensional  $(\cos\theta, p_t)$  bins according to the efficiencies obtained from the control sample, where  $\theta$  is the polar angle and  $p_t$  is the transverse momentum of the charged pions and leptons. The corrected detection efficiency is taken as the nominal result. The difference in efficiencies before and after the correction is taken as the systematic uncertainty due to tracking. It is assigned to be 0.4% for each pion and 0.1% for each lepton, resulting in a total tracking uncertainty of 1.0%.
- (iii) Photon detection: The photon detection efficiency has been studied using a control sample of  $e^+e^- \rightarrow \gamma\mu^+\mu^-$ . The difference between data and MC simulation is found to be 0.5% for each photon. Therefore, the total systematic uncertainty for two photons is assigned as 1.0%.
- (iv)  $\pi^0$  reconstruction: Using a high purity control sample of  $J/\psi \rightarrow \pi^0 p\bar{p}$ , the systematic uncertainty from  $\pi^0$  reconstruction is determined to be 1.0% [38].
- (v) Kinematic fit:  $\epsilon_{\text{sig}}$  is the efficiency obtained from the signal MC sample after the helix parameter correction. The systematic uncertainty related to the kinematic fit is evaluated by comparing the efficiencies with and without this correction [39]. Half of their difference, 0.7%, is taken as the associated uncertainty.
- (vi) Quoted BFs: The quoted BFs of  $J/\psi \rightarrow e^+e^-$ ,  $J/\psi \rightarrow \mu^+\mu^-$ , and  $\pi^0 \rightarrow \gamma\gamma$  are taken from the PDG [4], with uncertainties of 0.5%, 0.6%, and 0.03%, respectively.
- (vii) Mass windows: To evaluate the systematic uncertainty associated with the choice of mass windows, we perform a Barlow test [40] to examine the

deviation in significance ( $\zeta$ ) between the baseline selection and that used for the systematic test. The deviation in significance is defined as

$$\zeta = \frac{|V_{\text{nominal}} - V_{\text{test}}|}{\sqrt{|\sigma_{V_{\text{nominal}}}^2 - \sigma_{V_{\text{test}}}^2|}}, \quad (2)$$

where  $V$  is  $N_{\text{sig}}^{\text{up}}/\epsilon_{\text{sig}}$ ;  $\sigma_V$  is the statistical uncertainty on  $V$ . The mass windows applied on  $M(\pi^+\pi^-)$  and  $M(\pi^0\pi^+\pi^-)$  are varied between (0.270, 0.330) GeV/ $c^2$  and (0.225, 0.305) GeV/ $c^2$  with steps of 3.0 MeV/ $c^2$  and 4.0 MeV/ $c^2$ , respectively. As the  $\zeta$  values are always smaller than 2, the corresponding systematic uncertainties are ignored.

(viii) Signal mode: Due to the limited knowledge of the  $M(\pi^+\pi^-)$  distribution in the decay  $h_c \rightarrow \pi^+\pi^-J/\psi$ , the signal MC sample is generated uniformly in phase space without considering the angular distribution in the nominal analysis. To account for the potential systematic bias of the theoretical model, an alternative signal MC sample is generated. In this model, pure  $P$ -wave production between the two-pion system ( $S$ -wave) and  $J/\psi$  is assumed, specifically  $h_c \rightarrow f_0(500)J/\psi$ , which is described by the helicity amplitude model in EVTGEN [31,32]. The decay  $f_0(500) \rightarrow \pi^+\pi^-$  is generated using a phase space model. The efficiency difference between these two models, 6.3%, is assigned as the systematic uncertainty.

The multiplicative systematic uncertainties are summarized in Table I. The total systematic uncertainty is obtained by adding all contributions in quadrature under the assumption that they are independent.

The additive systematic uncertainties stem from the determination of the signal yield, which depends on the fit range and signal and background shapes. Since these additive systematic uncertainties are correlated, we simultaneously change these three fit conditions and choose the

TABLE I. Multiplicative systematic uncertainties (%).

Source	Uncertainty
Number of $\psi(3686)$ events	0.5
Tracking	1.0
Photon detection	1.0
$\pi^0$ reconstruction	1.0
Kinematic fit	0.7
$M(\pi^+\pi^-)$ mass window	Neglected
$M(\pi^+\pi^-\pi^0)$ mass window	Neglected
$B(\pi^0 \rightarrow \gamma\gamma)$	Neglected
$B(J/\psi \rightarrow e^+e^-)$	0.5
$B(J/\psi \rightarrow \mu^+\mu^-)$	0.6
Signal model	6.3
Total	6.6

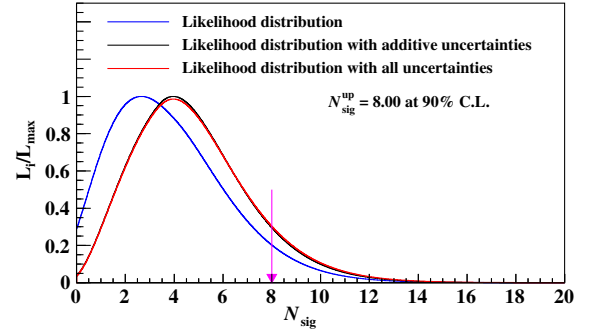


FIG. 3. The normalized likelihood distribution for  $\psi(3686) \rightarrow \pi^0 h_c, h_c \rightarrow \pi^+\pi^-J/\psi$ . The result obtained without accounting for any systematic uncertainties is depicted in blue, another with additive systematic uncertainties in black, and the third considering all systematic uncertainties in red. The arrow indicates the upper limit on the signal yield at the 90% confidence level after accounting for all systematic uncertainties.

most conservative upper limit. The contributions to the systematic uncertainties are discussed below.

- (i) Fit range: The systematic uncertainty arising from the fit range is evaluated by varying the fit range, adjusting both left and right limits by  $\pm 10$  MeV/ $c^2$ .
- (ii) Signal shape: The systematic uncertainty from the signal shape is estimated by using the MC-simulated shape convolved with a Gaussian function. The parameters of the Gaussian function are  $M_{\text{Gaussian}} = -0.4 \pm 0.3$  MeV and  $\sigma_{\text{Gaussian}} = 0.7 \pm 1.0$  MeV, taken from  $e^+e^- \rightarrow \eta h_c, h_c \rightarrow \gamma \eta c$  [41].
- (iii) Background shape: The systematic uncertainty due to the background shape is estimated by replacing the ARGUS function [36] with a 0th-order polynomial function, or by fixing the background yield to the remaining inclusive MC sample.

The multiplicative and additive systematic uncertainties are incorporated into the calculation of the upper limit via [42,43]

$$L'(N) = \int_{\epsilon=0}^1 L\left(\frac{\epsilon}{\epsilon_{\text{sig}}}\right) \exp\left[-\frac{(\epsilon - \epsilon_{\text{sig}})^2}{2\sigma_\epsilon^2}\right] d\epsilon, \quad (3)$$

where  $L(N)$  is the likelihood distribution as a function of signal yield,  $N$ ;  $\epsilon$  is the expected efficiency and  $\epsilon_{\text{sig}}$  is the nominal efficiency;  $\sigma_\epsilon$  is its multiplicative systematic uncertainty as summarized in Table I. The likelihood distribution is shown in Fig. 3, note that the shift of the peak value is mostly due to the signal line shape uncertainty. The signal yield of the process  $\psi(3686) \rightarrow \pi^0 h_c, h_c \rightarrow \pi^+\pi^-J/\psi$  at the 90% CL, is taken as the upper limit ( $N_{\text{sig}}^{\text{up}} = 8.00$ ), and used for the calculation of the upper limit of BF.

## VI. SUMMARY

A search for the hadronic transition  $h_c \rightarrow \pi^+\pi^-J/\psi$  is performed by analyzing  $(2712.4 \pm 14.3) \times 10^6$   $\psi(3686)$

events collected at the BESIII experiment, no significant signal is observed. The upper limit on the product of BFs, that is  $\mathcal{B}(\psi(3686) \rightarrow \pi^0 h_c) \times \mathcal{B}(h_c \rightarrow \pi^+\pi^-J/\psi)$ , at the 90% CL is determined to be  $6.7 \times 10^{-7}$ .

Using the PDG value of  $\mathcal{B}(\psi(3686) \rightarrow \pi^0 h_c) = (7.4 \pm 0.5) \times 10^{-4}$  and incorporating the additional uncertainty of 6.8% [4], the upper limit for  $\mathcal{B}(h_c \rightarrow \pi^+\pi^-J/\psi)$  at the 90% CL is estimated to be  $9.4 \times 10^{-4}$ . This result is above the predicted upper limit of  $\mathcal{B}(h_c \rightarrow \pi^+\pi^-J/\psi)$  of  $1.2 \times 10^{-5}$  obtained from the latest result of  $\mathcal{B}(h_c \rightarrow \pi^0 J/\psi)$  [18] as proposed by Voloshin [15].

Neglecting the small difference between phase space for charged and neutral  $\pi\pi$  modes, we obtain  $\mathcal{B}(h_c \rightarrow \pi\pi J/\psi) < 1.41 \times 10^{-3}$  (including charged and neutral modes) at the 90% CL by considering isospin symmetry. The upper limit on the BF of  $h_c \rightarrow \pi\pi J/\psi$  presented in this paper is about 3 times lower than that from the previous study [17]. In comparison with theoretical predictions, our result is an order of magnitude smaller than the BF predicted by Kuang *et al.* (about 2%) [13], and closer to the prediction calculated by Pyungwon Ko (0.05%) [14].

### ACKNOWLEDGMENTS

The BESIII collaboration thanks the staff of BEPCII and the IHEP computing center for their strong support. This work is supported in part by National Key Research and Development Program of China under Contracts No. 2020YFA0406300, No. 2020YFA0406400; National Natural Science Foundation of China (NSFC) under Contracts No. 12375070, No. 11625523, No. 11635010,

No. 11735014, No. 11822506, No. 11835012, No. 11935015, No. 11935016, No. 11935018, No. 11961141012, No. 12022510, No. 12025502, No. 12035009, No. 12035013, No. 12061131003; The key scientific research Projects of colleges and universities in Henan Province (21A140012); the Chinese Academy of Sciences (CAS) Large-Scale Scientific Facility Program; Joint Large-Scale Scientific Facility Funds of the NSFC and CAS under Contracts No. U2032108, No. U1732263, No. U1832207; CAS Key Research Program of Frontier Sciences under Contract No. QYZDJ-SSW-SLH040; the CAS Center for Excellence in Particle Physics (CCEPP); Shanghai Leading Talent Program of Eastern Talent Plan under Contract No. JLH5913002; 100 Talents Program of CAS; INPAC and Shanghai Key Laboratory for Particle Physics and Cosmology; ERC under Contract No. 758462; European Union Horizon 2020 research and innovation programme under Contract No. Marie Skłodowska-Curie grant agreement No. 894790; German Research Foundation DFG under Contracts Nos. 443159800, Collaborative Research Center CRC 1044, FOR 2359, GRK 2149; Istituto Nazionale di Fisica Nucleare, Italy; Ministry of Development of Turkey under Contract No. DPT2006K-120470; National Science and Technology fund; Olle Engkvist Foundation under Contract No. 200-0605; STFC (United Kingdom); The Knut and Alice Wallenberg Foundation (Sweden) under Contract No. 2016.0157; The Royal Society, UK under Contracts Nos. DH140054, DH160214; The Swedish Research Council; U.S. Department of Energy under Contracts No. DE-FG02-05ER41374, No. DE-SC-0012069.

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M. Ablikim,<sup>1</sup> M. N. Achasov,<sup>4,c</sup> P. Adlarson,<sup>76</sup> O. Afedulidis,<sup>3</sup> X. C. Ai,<sup>81</sup> R. Aliberti,<sup>35</sup> A. Amoroso,<sup>75a,75c</sup> Y. Bai,<sup>57</sup> O. Bakina,<sup>36</sup> I. Balossino,<sup>29a</sup> Y. Ban,<sup>46,h</sup> H.-R. Bao,<sup>64</sup> V. Batzokskaya,<sup>1,44</sup> K. Begzsuren,<sup>32</sup> N. Berger,<sup>35</sup> M. Berlowski,<sup>44</sup> M. Bertani,<sup>28a</sup> D. Bettoni,<sup>29a</sup> F. Bianchi,<sup>75a,75c</sup> E. Bianco,<sup>75a,75c</sup> A. Bortone,<sup>75a,75c</sup> I. Boyko,<sup>36</sup> R. A. Briere,<sup>5</sup> A. Brueggemann,<sup>69</sup> H. Cai,<sup>77</sup> X. Cai,<sup>1,58</sup> A. Calcaterra,<sup>28a</sup> G. F. Cao,<sup>1,64</sup> N. Cao,<sup>1,64</sup> S. A. Cetin,<sup>62a</sup> X. Y. Chai,<sup>46,h</sup> J. F. Chang,<sup>1,58</sup> G. R. Che,<sup>43</sup> Y. Z. Che,<sup>1,58,64</sup> G. Chelkov,<sup>36,b</sup> C. Chen,<sup>43</sup> C. H. Chen,<sup>9</sup> Chao Chen,<sup>55</sup> G. Chen,<sup>1</sup> H. S. Chen,<sup>1,64</sup> H. Y. Chen,<sup>20</sup> M. L. Chen,<sup>1,58,64</sup> S. J. Chen,<sup>42</sup> S. L. Chen,<sup>45</sup> S. M. Chen,<sup>61</sup> T. Chen,<sup>1,64</sup> X. R. Chen,<sup>31,64</sup> X. T. Chen,<sup>1,64</sup> Y. B. Chen,<sup>1,58</sup> Y. Q. Chen,<sup>34</sup> Z. J. Chen,<sup>25,i</sup> S. K. Choi,<sup>10</sup> G. Cibinetto,<sup>29a</sup> F. Cossio,<sup>75c</sup> J. J. Cui,<sup>50</sup> H. L. Dai,<sup>1,58</sup> J. P. Dai,<sup>79</sup> A. Dbeyssi,<sup>18</sup> R. E. de Boer,<sup>3</sup> D. Dedovich,<sup>36</sup> C. Q. Deng,<sup>73</sup> Z. Y. Deng,<sup>1</sup> A. Denig,<sup>35</sup> I. Denysenko,<sup>36</sup> M. Destefanis,<sup>75a,75c</sup> F. De Mori,<sup>75a,75c</sup> B. Ding,<sup>67,1</sup> X. X. Ding,<sup>46,h</sup> Y. Ding,<sup>40</sup> Y. Ding,<sup>34</sup> J. Dong,<sup>1,58</sup> L. Y. Dong,<sup>1,64</sup> M. Y. Dong,<sup>1,58,64</sup> X. Dong,<sup>77</sup> M. C. Du,<sup>1</sup> S. X. Du,<sup>81</sup> Y. Y. Duan,<sup>55</sup> Z. H. Duan,<sup>42</sup> P. Egorov,<sup>36,b</sup> J. J. Fan,<sup>19</sup> Y. H. Fan,<sup>45</sup> J. Fang,<sup>1,58</sup> J. Fang,<sup>59</sup> S. S. Fang,<sup>1,64</sup> W. X. Fang,<sup>1</sup> Y. Fang,<sup>1</sup> Y. Q. Fang,<sup>1,58</sup> R. Farinelli,<sup>29a</sup> L. Fava,<sup>75b,75c</sup> F. Feldbauer,<sup>3</sup> G. Felici,<sup>28a</sup> C. Q. Feng,<sup>72,58</sup> J. H. Feng,<sup>59</sup> Y. T. Feng,<sup>72,58</sup> M. Fritsch,<sup>3</sup> C. D. Fu,<sup>1</sup> J. L. Fu,<sup>64</sup> Y. W. Fu,<sup>1,64</sup> H. Gao,<sup>64</sup> X. B. Gao,<sup>41</sup> Y. N. Gao,<sup>19</sup> Y. N. Gao,<sup>46,h</sup> Yang Gao,<sup>72,58</sup> S. Garbolino,<sup>75c</sup> I. Garzia,<sup>29a,29b</sup> P. T. Ge,<sup>19</sup> Z. W. Ge,<sup>42</sup> C. Geng,<sup>59</sup> E. M. Gersabeck,<sup>68</sup> A. Gilman,<sup>70</sup> K. Goetzen,<sup>13</sup> L. Gong,<sup>40</sup> W. X. Gong,<sup>1,58</sup> W. Gradl,<sup>35</sup> S. Gramigna,<sup>29a,29b</sup> M. Greco,<sup>75a,75c</sup> M. H. Gu,<sup>1,58</sup> Y. T. Gu,<sup>15</sup> C. Y. Guan,<sup>1,64</sup> A. Q. Guo,<sup>31,64</sup> L. B. Guo,<sup>41</sup> M. J. Guo,<sup>50</sup> R. P. Guo,<sup>49</sup> Y. P. Guo,<sup>12,g</sup> A. Guskov,<sup>36,b</sup> J. Gutierrez,<sup>27</sup> K. L. Han,<sup>64</sup> T. T. Han,<sup>1</sup> F. Hanisch,<sup>3</sup> X. Q. Hao,<sup>19</sup> F. A. Harris,<sup>66</sup> K. K. He,<sup>55</sup> K. L. He,<sup>1,64</sup> F. H. Heinsius,<sup>3</sup> C. H. Heinz,<sup>35</sup> Y. K. Heng,<sup>1,58,64</sup> C. Herold,<sup>60</sup> T. Holtmann,<sup>3</sup> P. C. Hong,<sup>34</sup> G. Y. Hou,<sup>1,64</sup> X. T. Hou,<sup>1,64</sup> Y. R. Hou,<sup>64</sup> Z. L. Hou,<sup>1</sup> B. Y. Hu,<sup>59</sup> H. M. Hu,<sup>1,64</sup> J. F. Hu,<sup>56,j</sup> Q. P. Hu,<sup>72,58</sup> S. L. Hu,<sup>12,g</sup> T. Hu,<sup>1,58,64</sup> Y. Hu,<sup>1</sup> G. S. Huang,<sup>72,58</sup> K. X. Huang,<sup>59</sup> L. Q. Huang,<sup>31,64</sup> P. Huang,<sup>42</sup> X. T. Huang,<sup>50</sup> Y. P. 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C. Liu,<sup>34</sup> C. X. Liu,<sup>1</sup> F. Liu,<sup>1</sup> F. H. Liu,<sup>53</sup> Feng Liu,<sup>6</sup> G. M. Liu,<sup>56j</sup> H. Liu,<sup>38,k,l</sup> H. B. Liu,<sup>15</sup> H. H. Liu,<sup>1</sup> H. M. Liu,<sup>1,64</sup> Huihui Liu,<sup>21</sup> J. B. Liu,<sup>72,58</sup> J. Y. Liu,<sup>1,64</sup> K. Liu,<sup>38,k,l</sup> K. Y. Liu,<sup>40</sup> Ke Liu,<sup>22</sup> L. Liu,<sup>72,58</sup> L. C. Liu,<sup>43</sup> Lu Liu,<sup>43</sup> M. H. Liu,<sup>12,g</sup> P. L. Liu,<sup>1</sup> Q. Liu,<sup>64</sup> S. B. Liu,<sup>72,58</sup> T. Liu,<sup>12,g</sup> W. K. Liu,<sup>43</sup> W. M. Liu,<sup>72,58</sup> X. Liu,<sup>39</sup> X. Liu,<sup>38,k,l</sup> Y. Liu,<sup>38,k,l</sup> Y. Liu,<sup>81</sup> Y. B. Liu,<sup>43</sup> Z. A. Liu,<sup>1,58,64</sup> Z. D. Liu,<sup>9</sup> Z. Q. Liu,<sup>50</sup> X. C. Lou,<sup>1,58,64</sup> F. X. Lu,<sup>59</sup> H. J. Lu,<sup>23</sup> J. G. Lu,<sup>1,58</sup> Y. Lu,<sup>7</sup> Y. P. Lu,<sup>1,58</sup> Z. H. Lu,<sup>1,64</sup> C. L. Luo,<sup>41</sup> J. R. Luo,<sup>59</sup> M. X. Luo,<sup>80</sup> T. Luo,<sup>12,g</sup> X. L. Luo,<sup>1,58</sup> X. R. Lyu,<sup>64</sup> Y. F. Lyu,<sup>43</sup> F. C. Ma,<sup>40</sup> H. Ma,<sup>79</sup> H. L. Ma,<sup>1</sup> J. L. Ma,<sup>1,64</sup> L. L. Ma,<sup>50</sup> L. R. Ma,<sup>67</sup> M. M. Ma,<sup>1,64</sup> Q. M. Ma,<sup>1</sup> R. Q. Ma,<sup>1,64</sup> R. Y. Ma,<sup>19</sup> T. Ma,<sup>72,58</sup> X. T. Ma,<sup>1,64</sup> X. Y. Ma,<sup>1,58</sup> Y. M. Ma,<sup>31</sup> F. E. Maas,<sup>18</sup> I. MacKay,<sup>70</sup> M. Maggiora,<sup>75a,75c</sup> S. Malde,<sup>70</sup> Y. J. Mao,<sup>46,h</sup> Z. P. Mao,<sup>1</sup> S. Marcello,<sup>75a,75c</sup> Y. H. Meng,<sup>64</sup> Z. X. Meng,<sup>67</sup> J. G. Messchendorp,<sup>13,65</sup> G. Mezzadri,<sup>29a</sup> H. Miao,<sup>1,64</sup> T. J. Min,<sup>42</sup> R. E. Mitchell,<sup>27</sup> X. H. Mo,<sup>1,58,64</sup> B. Moses,<sup>27</sup> N. Yu. Muchnoi,<sup>4,c</sup> J. Muskalla,<sup>35</sup> Y. Nefedov,<sup>36</sup> F. Nerling,<sup>18,e</sup> L. S. Nie,<sup>20</sup> I. B. Nikolaev,<sup>4,c</sup> Z. Ning,<sup>1,58</sup> S. Nisar,<sup>11,m</sup> Q. L. Niu,<sup>38,k,l</sup> W. D. Niu,<sup>55</sup> Y. Niu,<sup>50</sup> S. L. Olsen,<sup>64</sup> S. L. Olsen,<sup>10,64</sup> Q. Ouyang,<sup>1,58,64</sup> S. Pacetti,<sup>28b,28c</sup> X. Pan,<sup>55</sup> Y. Pan,<sup>57</sup> A. Pathak,<sup>10</sup> A. Pathak,<sup>34</sup> Y. P. Pei,<sup>72,58</sup> M. Pelizaeus,<sup>3</sup> H. P. Peng,<sup>72,58</sup> Y. Y. Peng,<sup>38,k,l</sup> K. Peters,<sup>13,e</sup> J. L. Ping,<sup>41</sup> R. G. Ping,<sup>1,64</sup> S. Plura,<sup>35</sup> V. Prasad,<sup>33</sup> F. Z. Qi,<sup>1</sup> H. Qi,<sup>72,58</sup> H. R. Qi,<sup>61</sup> M. Qi,<sup>42</sup> S. Qian,<sup>1,58</sup> W. B. Qian,<sup>64</sup> C. F. Qiao,<sup>64</sup> J. H. Qiao,<sup>19</sup> J. J. Qin,<sup>73</sup> L. Q. Qin,<sup>14</sup> L. Y. Qin,<sup>72,58</sup> X. P. Qin,<sup>12,g</sup> X. S. Qin,<sup>50</sup> Z. H. Qin,<sup>1,58</sup> J. F. Qiu,<sup>1</sup> Z. H. Qu,<sup>73</sup> C. F. Redmer,<sup>35</sup> K. J. Ren,<sup>39</sup> A. Rivetti,<sup>75c</sup> M. Rolo,<sup>75c</sup> G. Rong,<sup>1,64</sup> Ch. Rosner,<sup>18</sup> M. Q. Ruan,<sup>1,58</sup> S. N. Ruan,<sup>43</sup> N. Salone,<sup>44</sup> A. Sarantsev,<sup>36,d</sup> Y. Schelhaas,<sup>35</sup> K. Schoenning,<sup>76</sup> M. Scodreggio,<sup>29a</sup> K. Y. Shan,<sup>12,g</sup> W. Shan,<sup>24</sup> X. Y. Shan,<sup>72,58</sup> Z. J. Shang,<sup>38,k,l</sup> J. F. Shangguan,<sup>16</sup> L. G. Shao,<sup>1,64</sup> M. Shao,<sup>72,58</sup> C. P. Shen,<sup>12,g</sup> H. F. Shen,<sup>1,8</sup> W. H. Shen,<sup>64</sup> X. Y. Shen,<sup>1,64</sup> B. A. Shi,<sup>64</sup> H. Shi,<sup>72,58</sup> J. L. Shi,<sup>12,g</sup> J. Y. Shi,<sup>1</sup> S. Y. Shi,<sup>73</sup> X. Shi,<sup>1,58</sup> J. J. Song,<sup>19</sup> T. Z. Song,<sup>59</sup> W. M. Song,<sup>34,1</sup> Y. J. Song,<sup>12,g</sup> Y. X. Song,<sup>46,h,n</sup> S. Sosio,<sup>75a,75c</sup> S. Spataro,<sup>75a,75c</sup> F. Stieler,<sup>35</sup> S. S. Su,<sup>40</sup> Y. J. Su,<sup>64</sup> G. B. Sun,<sup>77</sup> G. X. Sun,<sup>1</sup> H. Sun,<sup>64</sup> H. K. Sun,<sup>1</sup> J. F. Sun,<sup>19</sup> K. Sun,<sup>61</sup> L. Sun,<sup>77</sup> S. S. Sun,<sup>1,64</sup> T. Sun,<sup>51,f</sup> Y. Sun,<sup>9</sup> Y. J. Sun,<sup>72,58</sup> Y. Z. Sun,<sup>1</sup> Z. Q. Sun,<sup>1,64</sup> Z. T. Sun,<sup>50</sup> C. J. Tang,<sup>54</sup> G. Y. Tang,<sup>1</sup> J. Tang,<sup>59</sup> M. Tang,<sup>72,58</sup> Y. A. Tang,<sup>77</sup> L. Y. Tao,<sup>73</sup> Q. T. Tao,<sup>25,i</sup> M. Tat,<sup>70</sup> J. X. Teng,<sup>72,58</sup> V. Thoren,<sup>76</sup> W. H. Tian,<sup>59</sup> Y. Tian,<sup>31,64</sup> Z. F. Tian,<sup>77</sup> I. Uman,<sup>62b</sup> Y. Wan,<sup>55</sup> S. J. Wang,<sup>50</sup> B. Wang,<sup>1</sup> Bo Wang,<sup>72,58</sup> C. Wang,<sup>19</sup> D. Y. Wang,<sup>46,h</sup> H. J. Wang,<sup>38,k,l</sup> J. J. Wang,<sup>77</sup> J. P. Wang,<sup>50</sup> K. Wang,<sup>1,58</sup> L. L. Wang,<sup>1</sup> M. Wang,<sup>50</sup> N. Y. Wang,<sup>64</sup> S. Wang,<sup>38,k,l</sup> S. Wang,<sup>12,g</sup> T. Wang,<sup>12,g</sup> T. J. Wang,<sup>43</sup> W. Wang,<sup>73</sup> W. Wang,<sup>59</sup> W. P. Wang,<sup>35,58,72,o</sup> X. Wang,<sup>46,h</sup> X. F. Wang,<sup>38,k,l</sup> X. J. Wang,<sup>39</sup> X. L. Wang,<sup>12,g</sup> X. N. Wang,<sup>1</sup> Y. Wang,<sup>61</sup> Y. D. Wang,<sup>45</sup> Y. F. Wang,<sup>1,58,64</sup> Y. H. Wang,<sup>38,k,l</sup> Y. L. Wang,<sup>19</sup> Y. N. Wang,<sup>45</sup> Y. Q. Wang,<sup>1</sup> Yaqian Wang,<sup>17</sup> Yi Wang,<sup>61</sup> Z. Wang,<sup>1,58</sup> Z. L. Wang,<sup>73</sup> Z. Y. Wang,<sup>1,64</sup> D. H. Wei,<sup>14</sup> F. Weidner,<sup>69</sup> S. P. Wen,<sup>1</sup> Y. R. Wen,<sup>39</sup> U. Wiedner,<sup>3</sup> G. Wilkinson,<sup>70</sup> M. Wolke,<sup>76</sup> L. Wollenberg,<sup>3</sup> C. Wu,<sup>39</sup> J. F. Wu,<sup>1,8</sup> L. H. Wu,<sup>1</sup> L. J. Wu,<sup>1,64</sup> Lianjie Wu,<sup>19</sup> X. Wu,<sup>12,g</sup> X. H. Wu,<sup>34</sup> Y. H. Wu,<sup>55</sup> Y. J. Wu,<sup>31</sup> Z. Wu,<sup>1,58</sup> L. Xia,<sup>72,58</sup> X. M. Xian,<sup>39</sup> B. H. Xiang,<sup>1,64</sup> T. Xiang,<sup>46,h</sup> D. Xiao,<sup>38,k,l</sup> G. Y. Xiao,<sup>42</sup> H. Xiao,<sup>73</sup> S. Y. Xiao,<sup>1</sup> Y. L. Xiao,<sup>12,g</sup> Z. J. Xiao,<sup>41</sup> C. Xie,<sup>42</sup> X. H. Xie,<sup>46,h</sup> Y. Xie,<sup>50</sup> Y. G. Xie,<sup>1,58</sup> Y. H. Xie,<sup>6</sup> Z. P. Xie,<sup>72,58</sup> T. Y. Xing,<sup>1,64</sup> C. F. Xu,<sup>1,64</sup> C. J. Xu,<sup>59</sup> G. F. Xu,<sup>1</sup> M. Xu,<sup>72,58</sup> Q. J. Xu,<sup>16</sup> Q. N. Xu,<sup>30</sup> W. Xu,<sup>1</sup> W. L. Xu,<sup>67</sup> X. P. Xu,<sup>55</sup> Y. Xu,<sup>40</sup> Y. C. Xu,<sup>78</sup> Z. S. Xu,<sup>64</sup> F. Yan,<sup>12,g</sup> L. Yan,<sup>12,g</sup> W. B. Yan,<sup>72,58</sup> W. C. Yan,<sup>81</sup> W. P. Yan,<sup>19</sup> X. Q. Yan,<sup>1,64</sup> H. J. Yang,<sup>51,f</sup> H. L. Yang,<sup>34</sup> H. X. Yang,<sup>1</sup> J. H. Yang,<sup>42</sup> R. J. Yang,<sup>19</sup> T. Yang,<sup>1</sup> Y. Yang,<sup>12,g</sup> Y. F. Yang,<sup>1,64</sup> Y. F. Yang,<sup>43</sup> Y. X. Yang,<sup>1,64</sup> Y. Z. Yang,<sup>19</sup> Z. W. Yang,<sup>38,k,l</sup> Z. P. Yao,<sup>50</sup> M. Ye,<sup>1,58</sup> M. H. Ye,<sup>8</sup> J. H. Yin,<sup>1</sup> Junhao Yin,<sup>43</sup> Z. Y. You,<sup>59</sup> B. X. Yu,<sup>1,58,64</sup> C. X. Yu,<sup>43</sup> G. Yu,<sup>1,64</sup> J. S. Yu,<sup>25,i</sup> M. C. Yu,<sup>40</sup> T. Yu,<sup>73</sup> X. D. Yu,<sup>46,h</sup> C. Z. Yuan,<sup>1,64</sup> J. Yuan,<sup>34</sup> J. Yuan,<sup>45</sup> L. Yuan,<sup>2</sup> S. C. Yuan,<sup>1,64</sup> Y. Yuan,<sup>1,64</sup> Z. Y. Yuan,<sup>59</sup> C. X. Yue,<sup>39</sup> Ying Yue,<sup>19</sup> A. A. Zafar,<sup>74</sup> F. R. Zeng,<sup>50</sup> S. H. Zeng,<sup>63</sup> X. Zeng,<sup>12,g</sup> Y. Zeng,<sup>25,i</sup> Y. J. Zeng,<sup>59</sup> Y. J. Zeng,<sup>1,64</sup> X. Y. Zhai,<sup>34</sup> Y. C. Zhai,<sup>50</sup> Y. H. Zhan,<sup>59</sup> A. Q. Zhang,<sup>1,64</sup> B. L. Zhang,<sup>1,64</sup> B. X. Zhang,<sup>1</sup> D. H. Zhang,<sup>43</sup> G. Y. Zhang,<sup>19</sup> H. Zhang,<sup>81</sup> H. Zhang,<sup>72,58</sup> H. C. Zhang,<sup>1,58,64</sup> H. H. Zhang,<sup>59</sup> H. Q. Zhang,<sup>1,58,64</sup> H. R. Zhang,<sup>72,58</sup> H. Y. Zhang,<sup>1,58</sup> J. Zhang,<sup>81</sup> J. Zhang,<sup>59</sup> J. J. Zhang,<sup>52</sup> J. L. Zhang,<sup>20</sup> J. Q. Zhang,<sup>41</sup> J. S. Zhang,<sup>12,g</sup> J. W. Zhang,<sup>1,58,64</sup> J. X. Zhang,<sup>38,k,l</sup> J. Y. Zhang,<sup>1</sup> J. Z. Zhang,<sup>1,64</sup> Jianyu Zhang,<sup>64</sup> L. M. Zhang,<sup>61</sup> Lei Zhang,<sup>42</sup> P. Zhang,<sup>1,64</sup> Q. Zhang,<sup>19</sup> Q. Y. Zhang,<sup>34</sup> R. Y. Zhang,<sup>38,k,l</sup> S. H. Zhang,<sup>1,64</sup> Shulei Zhang,<sup>25,i</sup> X. M. Zhang,<sup>1</sup> X. Y. Zhang,<sup>40</sup> X. Y. Zhang,<sup>50</sup> Y. Zhang,<sup>73</sup> Y. Zhang,<sup>1</sup> Y. T. Zhang,<sup>81</sup> Y. H. Zhang,<sup>1,58</sup> Y. M. Zhang,<sup>39</sup> Yan Zhang,<sup>72,58</sup> Z. D. Zhang,<sup>1</sup> Z. H. Zhang,<sup>1</sup> Z. L. Zhang,<sup>34</sup> Z. X. Zhang,<sup>19</sup> Z. Y. Zhang,<sup>43</sup> Z. Y. Zhang,<sup>77</sup> Z. Z. Zhang,<sup>45</sup> Zh. Zh. Zhang,<sup>19</sup> G. Zhao,<sup>1</sup> J. Y. Zhao,<sup>1,64</sup> J. Z. Zhao,<sup>1,58</sup> L. Zhao,<sup>1</sup> Lei Zhao,<sup>72,58</sup> M. G. Zhao,<sup>43</sup> N. Zhao,<sup>79</sup> R. P. Zhao,<sup>64</sup> S. J. Zhao,<sup>81</sup> Y. B. Zhao,<sup>1,58</sup> Y. X. Zhao,<sup>31,64</sup> Z. G. Zhao,<sup>72,58</sup> A. Zhemchugov,<sup>36,b</sup> B. Zheng,<sup>73</sup> B. M. Zheng,<sup>34</sup> J. P. Zheng,<sup>1,58</sup> W. J. Zheng,<sup>1,64</sup> X. R. Zheng,<sup>19</sup> Y. H. Zheng,<sup>64</sup> B. Zhong,<sup>41</sup> X. Zhong,<sup>59</sup> H. Zhou,<sup>50</sup> J. Y. Zhou,<sup>34</sup> L. P. Zhou,<sup>1,64</sup> S. Zhou,<sup>6</sup> X. Zhou,<sup>77</sup> X. K. Zhou,<sup>6</sup> X. R. Zhou,<sup>72,58</sup> X. Y. Zhou,<sup>39</sup> Y. Z. Zhou,<sup>12,g</sup> Z. C. Zhou,<sup>20</sup> A. N. Zhu,<sup>64</sup> J. Zhu,<sup>43</sup> K. Zhu,<sup>1</sup> K. J. Zhu,<sup>1,58,64</sup> K. S. Zhu,<sup>12,g</sup> L. Zhu,<sup>34</sup> L. X. Zhu,<sup>64</sup> S. H. Zhu,<sup>71</sup> T. J. Zhu,<sup>12,g</sup> W. D. Zhu,<sup>41</sup> W. Z. Zhu,<sup>19</sup> Y. C. Zhu,<sup>72,58</sup> Z. A. Zhu,<sup>1,64</sup> J. H. Zou,<sup>1</sup> and J. Zu<sup>72,58</sup>

(BESIII Collaboration)

- <sup>1</sup>*Institute of High Energy Physics, Beijing 100049, People's Republic of China*  
<sup>2</sup>*Beihang University, Beijing 100191, People's Republic of China*  
<sup>3</sup>*Bochum Ruhr-University, D-44780 Bochum, Germany*  
<sup>4</sup>*Budker Institute of Nuclear Physics SB RAS (BINP), Novosibirsk 630090, Russia*  
<sup>5</sup>*Carnegie Mellon University, Pittsburgh, Pennsylvania 15213, USA*  
<sup>6</sup>*Central China Normal University, Wuhan 430079, People's Republic of China*  
<sup>7</sup>*Central South University, Changsha 410083, People's Republic of China*  
<sup>8</sup>*China Center of Advanced Science and Technology, Beijing 100190, People's Republic of China*  
<sup>9</sup>*China University of Geosciences, Wuhan 430074, People's Republic of China*  
<sup>10</sup>*Chung-Ang University, Seoul, 06974, Republic of Korea*  
<sup>11</sup>*COMSATS University Islamabad,  
Lahore Campus, Defence Road, Off Raiwind Road, 54000 Lahore, Pakistan*  
<sup>12</sup>*Fudan University, Shanghai 200433, People's Republic of China*  
<sup>13</sup>*GSI Helmholtzcentre for Heavy Ion Research GmbH, D-64291 Darmstadt, Germany*  
<sup>14</sup>*Guangxi Normal University, Guilin 541004, People's Republic of China*  
<sup>15</sup>*Guangxi University, Nanning 530004, People's Republic of China*  
<sup>16</sup>*Hangzhou Normal University, Hangzhou 310036, People's Republic of China*  
<sup>17</sup>*Hebei University, Baoding 071002, People's Republic of China*  
<sup>18</sup>*Helmholtz Institute Mainz, Staudinger Weg 18, D-55099 Mainz, Germany*  
<sup>19</sup>*Henan Normal University, Xinxiang 453007, People's Republic of China*  
<sup>20</sup>*Henan University, Kaifeng 475004, People's Republic of China*  
<sup>21</sup>*Henan University of Science and Technology, Luoyang 471003, People's Republic of China*  
<sup>22</sup>*Henan University of Technology, Zhengzhou 450001, People's Republic of China*  
<sup>23</sup>*Huangshan College, Huangshan 245000, People's Republic of China*  
<sup>24</sup>*Hunan Normal University, Changsha 410081, People's Republic of China*  
<sup>25</sup>*Hunan University, Changsha 410082, People's Republic of China*  
<sup>26</sup>*Indian Institute of Technology Madras, Chennai 600036, India*  
<sup>27</sup>*Indiana University, Bloomington, Indiana 47405, USA*  
<sup>28a</sup>*INFN Laboratori Nazionali di Frascati, I-00044, Frascati, Italy*  
<sup>28b</sup>*INFN Sezione di Perugia, I-06100, Perugia, Italy*  
<sup>28c</sup>*University of Perugia, I-06100, Perugia, Italy*  
<sup>29a</sup>*INFN Sezione di Ferrara, I-44122, Ferrara, Italy*  
<sup>29b</sup>*University of Ferrara, I-44122, Ferrara, Italy*  
<sup>30</sup>*Inner Mongolia University, Hohhot 010021, People's Republic of China*  
<sup>31</sup>*Institute of Modern Physics, Lanzhou 730000, People's Republic of China*  
<sup>32</sup>*Institute of Physics and Technology, Peace Avenue 54B, Ulaanbaatar 13330, Mongolia*  
<sup>33</sup>*Instituto de Alta Investigación, Universidad de Tarapacá, Casilla 7D, Arica 1000000, Chile*  
<sup>34</sup>*Jilin University, Changchun 130012, People's Republic of China*  
<sup>35</sup>*Johannes Gutenberg University of Mainz, Johann-Joachim-Becher-Weg 45, D-55099 Mainz, Germany*  
<sup>36</sup>*Joint Institute for Nuclear Research, 141980 Dubna, Moscow region, Russia*  
<sup>37</sup>*Justus-Liebig-Universitaet Giessen,  
II. Physikalisches Institut, Heinrich-Buff-Ring 16, D-35392 Giessen, Germany*  
<sup>38</sup>*Lanzhou University, Lanzhou 730000, People's Republic of China*  
<sup>39</sup>*Liaoning Normal University, Dalian 116029, People's Republic of China*  
<sup>40</sup>*Liaoning University, Shenyang 110036, People's Republic of China*  
<sup>41</sup>*Nanjing Normal University, Nanjing 210023, People's Republic of China*  
<sup>42</sup>*Nanjing University, Nanjing 210093, People's Republic of China*  
<sup>43</sup>*Nankai University, Tianjin 300071, People's Republic of China*  
<sup>44</sup>*National Centre for Nuclear Research, Warsaw 02-093, Poland*  
<sup>45</sup>*North China Electric Power University, Beijing 102206, People's Republic of China*  
<sup>46</sup>*Peking University, Beijing 100871, People's Republic of China*  
<sup>47</sup>*Qufu Normal University, Qufu 273165, People's Republic of China*  
<sup>48</sup>*Renmin University of China, Beijing 100872, People's Republic of China*  
<sup>49</sup>*Shandong Normal University, Jinan 250014, People's Republic of China*  
<sup>50</sup>*Shandong University, Jinan 250100, People's Republic of China*  
<sup>51</sup>*Shanghai Jiao Tong University, Shanghai 200240, People's Republic of China*  
<sup>52</sup>*Shanxi Normal University, Linfen 041004, People's Republic of China*  
<sup>53</sup>*Shanxi University, Taiyuan 030006, People's Republic of China*  
<sup>54</sup>*Sichuan University, Chengdu 610064, People's Republic of China*

- <sup>55</sup>*Soochow University, Suzhou 215006, People's Republic of China*
- <sup>56</sup>*South China Normal University, Guangzhou 510006, People's Republic of China*
- <sup>57</sup>*Southeast University, Nanjing 211100, People's Republic of China*
- <sup>58</sup>*State Key Laboratory of Particle Detection and Electronics, Beijing 100049, Hefei 230026, People's Republic of China*
- <sup>59</sup>*Sun Yat-Sen University, Guangzhou 510275, People's Republic of China*
- <sup>60</sup>*Suranaree University of Technology, University Avenue 111, Nakhon Ratchasima 30000, Thailand*
- <sup>61</sup>*Tsinghua University, Beijing 100084, People's Republic of China*
- <sup>62a</sup>*Turkish Accelerator Center Particle Factory Group, Istinye University, 34010, Istanbul, Turkey*
- <sup>62b</sup>*Near East University, Nicosia, North Cyprus, 99138, Mersin 10, Turkey*
- <sup>63</sup>*University of Bristol, H H Wills Physics Laboratory, Tyndall Avenue, Bristol, BS8 1TL, UK*
- <sup>64</sup>*University of Chinese Academy of Sciences, Beijing 100049, People's Republic of China*
- <sup>65</sup>*University of Groningen, NL-9747 AA Groningen, The Netherlands*
- <sup>66</sup>*University of Hawaii, Honolulu, Hawaii 96822, USA*
- <sup>67</sup>*University of Jinan, Jinan 250022, People's Republic of China*
- <sup>68</sup>*University of Manchester, Oxford Road, Manchester, M13 9PL, United Kingdom*
- <sup>69</sup>*University of Muenster, Wilhelm-Klemm-Strasse 9, 48149 Muenster, Germany*
- <sup>70</sup>*University of Oxford, Keble Road, Oxford OX13RH, United Kingdom*
- <sup>71</sup>*University of Science and Technology Liaoning, Anshan 114051, People's Republic of China*
- <sup>72</sup>*University of Science and Technology of China, Hefei 230026, People's Republic of China*
- <sup>73</sup>*University of South China, Hengyang 421001, People's Republic of China*
- <sup>74</sup>*University of the Punjab, Lahore-54590, Pakistan*
- <sup>75a</sup>*University of Turin and INFN, University of Turin, I-10125, Turin, Italy*
- <sup>75b</sup>*University of Eastern Piedmont, I-15121, Alessandria, Italy*
- <sup>75b</sup>*INFN, I-10125, Turin, Italy*
- <sup>76</sup>*Uppsala University, Box 516, SE-75120 Uppsala, Sweden*
- <sup>77</sup>*Wuhan University, Wuhan 430072, People's Republic of China*
- <sup>78</sup>*Yantai University, Yantai 264005, People's Republic of China*
- <sup>79</sup>*Yunnan University, Kunming 650500, People's Republic of China*
- <sup>80</sup>*Zhejiang University, Hangzhou 310027, People's Republic of China*
- <sup>81</sup>*Zhengzhou University, Zhengzhou 450001, People's Republic of China*

<sup>a</sup>Deceased.

<sup>b</sup>Also at the Moscow Institute of Physics and Technology, Moscow 141700, Russia.

<sup>c</sup>Also at the Novosibirsk State University, Novosibirsk, 630090, Russia.

<sup>d</sup>Also at the NRC "Kurchatov Institute", PNPI, 188300, Gatchina, Russia.

<sup>e</sup>Also at Goethe University Frankfurt, 60323 Frankfurt am Main, Germany.

<sup>f</sup>Also at Key Laboratory for Particle Physics, Astrophysics and Cosmology, Ministry of Education; Shanghai Key Laboratory for Particle Physics and Cosmology; Institute of Nuclear and Particle Physics, Shanghai 200240, People's Republic of China.

<sup>g</sup>Also at Key Laboratory of Nuclear Physics and Ion-beam Application (MOE) and Institute of Modern Physics, Fudan University, Shanghai 200443, People's Republic of China.

<sup>h</sup>Also at State Key Laboratory of Nuclear Physics and Technology, Peking University, Beijing 100871, People's Republic of China.

<sup>i</sup>Also at School of Physics and Electronics, Hunan University, Changsha 410082, China.

<sup>j</sup>Also at Guangdong Provincial Key Laboratory of Nuclear Science, Institute of Quantum Matter, South China Normal University, Guangzhou 510006, China.

<sup>k</sup>Also at MOE Frontiers Science Center for Rare Isotopes, Lanzhou University, Lanzhou 730000, People's Republic of China.

<sup>l</sup>Also at Lanzhou Center for Theoretical Physics, Lanzhou University, Lanzhou 730000, People's Republic of China.

<sup>m</sup>Also at the Department of Mathematical Sciences, IBA, Karachi 75270, Pakistan.

<sup>n</sup>Also at Ecole Polytechnique Federale de Lausanne (EPFL), CH-1015 Lausanne, Switzerland.

<sup>o</sup>Also at Helmholtz Institute Mainz, Staudinger Weg 18, D-55099 Mainz, Germany.