

Search for a 1^{-+} molecular state via $e^+e^- \rightarrow \gamma D_s^+ D_{s1}^-(2536) + \text{c.c.}$

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We search, for the first time, for an exotic molecular state with quantum numbers $J^{PC} = 1^{-+}$, called X , via the process $e^+e^- \rightarrow \gamma D_s^+ D_{s1}^-(2536) + \text{c.c.}$ using data samples corresponding to a luminosity of 5.8 fb^{-1} across center-of-mass energies from 4.612 to 4.951 GeV, collected with the BESIII detector operating at the BEPCII Collider. No statistically significant signal is observed. The upper limits on the product of cross section and branching fraction $\sigma(e^+e^- \rightarrow \gamma X) \cdot \mathcal{B}(X \rightarrow D_s^+ D_{s1}^-(2536) + \text{c.c.})$ at 90% confidence level are reported for each energy point, assuming the X mass to be $4.503 \text{ GeV}/c^2$ and the width 25, 50, 75, and 100 MeV, respectively.

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I. INTRODUCTION

Since their discovery two decades ago [1], the charmoniumlike states, known as XYZ, have enormously broadened our understanding of the hadronic mass spectrum. Unlike the conventional charmonium states, which are composed of charm quark antiquark pairs ($c\bar{c}$), the XYZ states are believed to present a more complex internal structure, including, e.g., tetraquark, molecule, or hybrid. Therefore, they provide additional information that goes beyond the traditional $c\bar{c}$ systems. The investigation of their spectrum, quantum numbers, production rate, and decays can shed light on the mechanisms of the strong interaction.

Since the charmoniumlike states have the same quantum numbers as the charmonium states, they are difficult to distinguish. For instance, the $X(3872)$ was first observed in the $B^\pm \rightarrow K^\pm \pi^+ \pi^- J/\psi$ decay by Belle [2] in 2003 and subsequently confirmed by several other experiments [3–5]. While $X(3872)$ is believed to be the first exotic charmoniumlike particle [6–12], there remains a long-standing debate about whether it could instead be the conventional $\chi_{c1}(2P)$ state [9]. Similarly, the vector state $Y(4230)$, which was observed and subsequently confirmed in its decay to $\pi^+ \pi^- J/\psi$ [13–15]; there are ongoing arguments suggesting that it could be the charmonium $\psi(4S)$ state [16–19] or an exotic state [20–24].

One possible way to bypass the aforementioned difficulty is to search for states that are “more exotic than the

other exotic states.” The $Z_c^\pm(3900)$ [25] is one kind of these states since it is charged and contains a $c\bar{c}$ component. In between the light meson states, the $\pi_1(1400)$ [26–30], $\pi_1(1600)$ [31,32], and $\eta_1(1855)$ [33] are considered exotic states due to their unusual quantum numbers $J^{PC} = 1^{-+}$, indicating non- $q\bar{q}$ quark components. Exotic states with unusual quantum numbers have been found only in the light-hadron spectrum, and up till now, no similar states have been discovered in the charmonium energy region, even if they are allowed by QCD. Reference [34] discusses the possibility that heavy-light meson states, such as $\bar{D}D_1(2420)$ and its charge conjugate (c.c.), can couple to states with exotic quantum numbers $J^{PC} = 1^{-+}$ in S -wave. Similarly, this can also be extended to D mesons with a strange quark, suggesting potential heavier exotic 1^{-+} states near the $D_s^+ D_{s1}^-(2536)$ threshold. Throughout this article without specification, the charge conjugated mode is implied.

In this article, the process $e^+e^- \rightarrow \gamma D_s^+ D_{s1}^-(2536)$ has been used to search for a molecular 1^{-+} state X , formed by $D_s^+ D_{s1}^-(2536)$. This has been done using twelve data samples with center-of-mass (c.m.) energies ($\sqrt{s}$) ranging from 4.612 to 4.951 GeV [35], corresponding to an integrated luminosity of 5.8 fb^{-1} . The values of c.m. energy and luminosity are listed in Table I.

II. BESIII DETECTOR AND MONTE CARLO SIMULATION

The BESIII detector [36] records symmetric e^+e^- collisions provided by the BEPCII storage ring [37] in the c.m. energy range from 1.84 to 4.95 GeV, with a peak luminosity of $1.1 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$ achieved at $\sqrt{s} = 3.773 \text{ GeV}$. BESIII has collected large data samples in this energy region [37]. The cylindrical core of the BESIII detector covers 93% of the full solid angle and

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TABLE I. The values used to determine $\sigma(e^+e^- \rightarrow \gamma X) \cdot \mathcal{B}(X \rightarrow D_s^+ D_{s1}^- (2536))$. Only the statistical uncertainty is presented, and the mass and width of the X candidate are set to be 4.503 GeV/ c^2 and 0.05 GeV, respectively. $\mathcal{L}_{\text{int}}$ is the integral luminosity, $(1 + \delta)$ is the radiative correction factor, $\frac{1}{|1 - \Pi|^2}$ is the VP factor, $\epsilon_{KK\pi}$ ($\epsilon_{K_S^0 K}$) is the selection efficiency of the $KK\pi$ ($K_S^0 K$) mode, $N_{KK\pi}$ is the number of signal events for the $KK\pi$ mode obtained by fitting, S is the statistical significance of the signal, $N_{KK\pi}^{\text{UL}}$ is the upper limit of the number of signals at 90% CL, and $\sigma^{\text{UL}} \cdot \mathcal{B}$ is the upper limit of the product of the cross section and the branching fraction at 90% CL.

$\sqrt{s}$ (GeV)	$\mathcal{L}_{\text{int}}$ (pb $^{-1}$)	$(1 + \delta)$	$\frac{1}{ 1 - \Pi ^2}$	$\epsilon_{KK\pi}(\%)$	$\epsilon_{K_S^0 K}(\%)$	$N_{KK\pi}$	S	$N_{KK\pi}^{\text{UL}}$	$\sigma^{\text{UL}} \cdot \mathcal{B}$ (pb)
4.612	103.7	0.689	1.055	4.47	8.04	$0.0^{+0.4}_{-0.0}$	0.1σ	1.7	26.8
4.628	521.5	0.734	1.054	4.27	7.66	$0.6^{+1.3}_{-0.7}$	0.1σ	2.8	8.6
4.641	551.7	0.751	1.054	4.03	7.36	$1.4^{+1.8}_{-1.0}$	1.8σ	5.4	16.0
4.661	529.4	0.773	1.054	2.60	4.61	$0.0^{+0.6}_{-0.0}$	0.3σ	2.8	13.1
4.682	1667.4	0.785	1.054	3.58	6.12	$7.0^{+3.5}_{-2.8}$	3.5σ	12.5	13.1
4.699	535.5	0.793	1.054	4.34	7.83	$2.2^{+1.6}_{-1.3}$	2.1σ	5.6	15.0
4.740	163.9	0.808	1.055	4.82	8.63	$0.0^{+0.4}_{-0.0}$	1.1σ	1.9	15.0
4.750	366.6	0.811	1.055	4.75	8.86	$0.5^{+2.2}_{-1.3}$	0.3σ	4.3	15.1
4.781	511.5	0.821	1.055	4.92	9.15	$0.0^{+0.5}_{-0.0}$	0.9σ	2.0	4.9
4.843	525.2	0.835	1.056	4.51	8.64	$0.0^{+0.4}_{-0.0}$	0.1σ	1.8	4.6
4.918	207.8	0.845	1.056	4.79	8.95	$2.0^{+1.8}_{-1.2}$	2.2σ	5.1	30.0
4.951	159.3	0.851	1.056	4.68	8.71	$0.0^{+0.4}_{-0.0}$	0.1σ	1.7	13.5

consists of a helium-based multilayer drift chamber (MDC), a plastic scintillator time-of-flight system (TOF), and a CsI(Tl) electromagnetic calorimeter (EMC), which are all enclosed in a superconducting solenoid magnet providing a 1.0 T magnetic field. The solenoid is supported by an octagonal flux-return yoke with resistive-plate counter-muon identification modules interleaved with the steel. The charged-particle momentum resolution at 1 GeV/ c is 0.5%, and the dE/dx resolution is 6% for electrons from Bhabha scattering. The EMC measures photon energies with a resolution of 2.5% (5%) at 1 GeV in the barrel (end cap) region. The time resolution in the TOF barrel region is 68 ps, while that in the end cap region is 110 ps. The end cap TOF system was upgraded in 2015 using multigap resistive-plate chamber technology, providing a time resolution of 60 ps, which benefits the total amount of the data used in this analysis [38].

Simulated data samples produced with a Geant4-based [39] Monte Carlo (MC) package, which includes the geometric description of the BESIII detector [40] and the detector response, are used to determine the detection efficiencies and estimate backgrounds. The simulation models the beam energy spread and ISR in the e^+e^- annihilation with the KKMC generator [41]. The inclusive MC sample includes the production of open charm processes, the ISR production of vector charmonium(like) states, and the continuum processes incorporated in KKMC [41]. All the known particle decays are modeled with EvtGen [42] using the branching fractions either taken from the Particle Data Group (PDG) [43] or estimated with Lundcharm [44]. The final-state radiation (FSR) from charged final-state particles is incorporated using the PHOTOS package [45].

We generate 200,000 signal MC events of $e^+e^- \rightarrow \gamma X$ and $X \rightarrow D_s^+ D_{s1}^- (2536)$ at each c.m. energy and each hypothetical X 's width with uniform phase space (PHSP) distribution. The X 's mass (M_X) is set to the $D_s^+ D_{s1}^- (2536)$ mass threshold 4.503 GeV/ c^2 , based on the molecule assumption that its mass should be very close to, perhaps a few MeV lower than, this threshold [34]; its width (Γ_X) is set to 25, 50, 75, and 100 MeV, reflecting the widths of the other charmoniumlike states. We generate the $D_s^+ \rightarrow K^+ K^- \pi^+$ decay based on the amplitude analysis results from Refs. [46–48], and the $D_s^+ \rightarrow K_S^0 K^+$ and $K_S^0 \rightarrow \pi^+ \pi^-$ decays according to the PHSP distribution. We generate $D_{s1}^- (2536) \rightarrow \bar{D}^{*0} K^-$ process via VVS-PWAVE model [42], with inclusive decays of $\bar{D}^{*0}$ following the world-averaged branching fractions [43], where $\bar{D}^{*0}$ decays 64.7% into $\bar{D}^0 \pi^0$ and 35.3% into $\bar{D}^0 \gamma$. The cross-section line shape is assumed to be proportional to E_γ^3/s [49], where E_γ is the energy of the radiative photon. This information is used to obtain the radiative correction factor and detection efficiency.

III. PRIMARY EVENT SELECTION

We employ a partial reconstruction method for the signal process $e^+e^- \rightarrow \gamma D_s^+ D_{s1}^- (2536)$, $D_{s1}^- (2536) \rightarrow \bar{D}^{*0} K^-$ to achieve higher efficiency. This method involves reconstructing the γ , D_s^+ , and a bachelor K^- from the $D_{s1}^- (2536)$ decay. The $D_{s1}^- (2536)$ and its daughter particle $\bar{D}^{*0}$ are searched for in the recoiling-mass spectrum of the γD_s^+ and $\gamma D_s^+ K^-$ candidates, respectively. The D_s^+ meson is reconstructed via $K^+ K^- \pi^+$ or $K_S^0 K^+$ with $K_S^0 \rightarrow \pi^+ \pi^-$.

Photon candidates are identified using showers in the EMC. The deposited energy of a shower must be greater

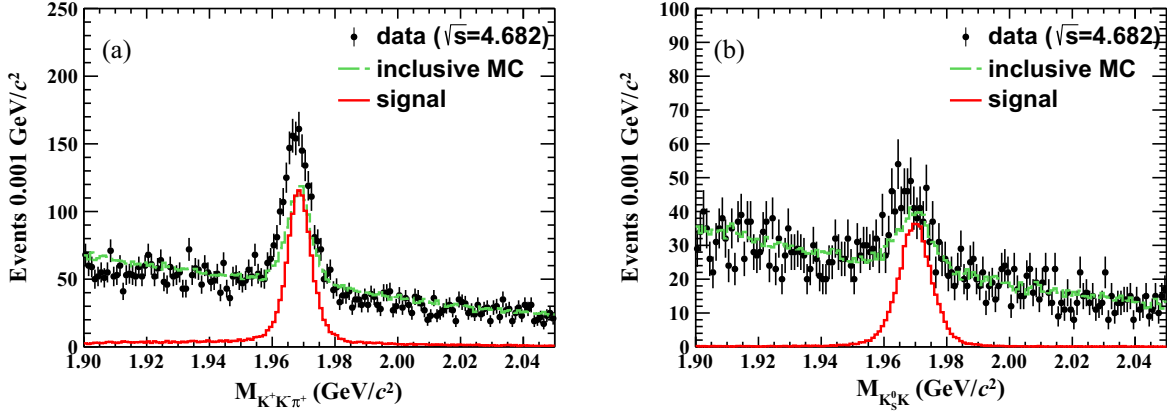


FIG. 1. Invariant-mass distributions of $M_{K^+K^-\pi^+}$ (a) and $M_{K_S^0K^+}$ (b) at $\sqrt{s} = 4.682$ GeV. Dots with error bars represent data, green dashed lines represent inclusive MC, and red solid lines indicate the signal. The number of events in the inclusive MC simulation is normalized to match the data, while the signal is normalized arbitrarily.

than 25 MeV in the barrel region ($|\cos\theta| < 0.80$) or greater than 50 MeV in the end cap region ($0.86 < |\cos\theta| < 0.92$). Here, θ is the polar angle with respect to the z axis, the symmetry axis of the MDC. To exclude showers that originate from charged tracks, the angle subtended by the EMC shower and the position of the closest charged track at the EMC must be greater than 10 degrees as measured from the interaction point (IP). To suppress the electronic noise and the showers unrelated to the event, the difference between the EMC time and the event start time is required to be within $[0, 700]$ ns [36]. The number of photons per event is required to be at least one.

A charged track is reconstructed from the hits in the MDC. We require that each charged track not associated with the K_S^0 must satisfy $|\cos\theta| < 0.93$, and the distance of the closest approach to the IP is within 10 cm along the z axis (V_z), and less than 1 cm in the transverse plane. Particle identification (PID) for charged tracks combines measurements of the energy deposited in the MDC (dE/dx) and the time-of-flight in the TOF to form likelihoods $\mathcal{L}(h)$ ($h = p, K, \pi$) for each hadron h hypothesis. Tracks are identified as $K^\pm$ ($\pi^\pm$) by comparing the likelihoods for the kaon and pion hypotheses, requiring $\mathcal{L}(K) > \mathcal{L}(\pi)$ and $\mathcal{L}(K) > 0$ [$\mathcal{L}(\pi) > \mathcal{L}(K)$ and $\mathcal{L}(\pi) > 0$].

Each K_S^0 candidate is reconstructed from two oppositely charged tracks that satisfy $|V_z| < 20$ cm and $|\cos\theta| < 0.93$. The two charged tracks are assigned as $\pi^+\pi^-$ without imposing any PID criteria. They are constrained to originate from a common vertex and are required to have an invariant mass within $|M_{\pi^+\pi^-} - m_{K_S^0}| < 9$ MeV/ c^2 , where $m_{K_S^0}$ is the K_S^0 nominal mass [43]. The decay length of the K_S^0 candidate is required to be greater than twice the vertex resolution away from the IP.

The selected $K^\pm$, $\pi^\pm$, and K_S^0 candidates in an event are combined to reconstruct $D_s^+ \rightarrow K^+K^-\pi^+$ or $D_s^+ \rightarrow K_S^0K^+$, denoted as the $KK\pi$ or K_S^0K modes, respectively. At least one K^- with opposite charge to the D_s^+ candidate is

required. Only the decays containing the intermediate states ϕ or $\bar{K}^*(892)^0$ in the $KK\pi$ mode are used to select the D_s^+ candidates. The invariant mass of K^+K^- ($K^+\pi^-$) is required to satisfy $|M_{K^+K^-} - m_\phi| < 9$ MeV/ c^2 ($|M_{K^+\pi^-} - m_{\bar{K}^*(892)^0}| < 66$ MeV/ c^2), corresponding to three standard deviations of the experimental mass resolution. The helicity angle of K^+ in the K^+K^- ($K^+\pi^-$) helicity frame is required to satisfy $|\cos\theta| > 0.36$ ($|\cos\theta| > 0.45$) to improve the significance of the D_s^+ meson. As an example, Fig. 1 shows the invariant-mass distributions of $K^+K^-\pi^+$ ($M_{K^+K^-\pi^+}$) and $K_S^0K^+$ ($M_{K_S^0K^+}$) at $\sqrt{s} = 4.682$ GeV. The D_s^+ candidates are ultimately selected using three standard deviations mass regions around the nominal D_s^+ mass, $|M_{K^+K^-\pi^+} - m_{D_s^+}| < 15$ MeV/ c^2 and $|M_{K_S^0K^+} - m_{D_s^+}| < 19$ MeV/ c^2 . Here and hereafter, m_y ($y = \phi, \bar{K}^*(892)^0, D_s^+$) denotes the respective nominal masses [43]. Since the resolutions and background levels are dependent on the c.m. energy, we categorize the data samples into three sets based on $\sqrt{s}$ to optimize the event selection criteria:

- (i) Set I: 4.612, 4.628, 4.641, 4.661, 4.682 GeV;
- (ii) Set II: 4.699, 4.740, 4.750, 4.781 GeV;
- (iii) Set III: 4.843, 4.918, 4.951 GeV.

Within a set, the resolutions and backgrounds are assumed to be similar for each energy point. To improve the resolution, the modified recoiling mass of $\gamma D_s^+ K^-$ is defined as $\text{RM}'_{D_s^+K^-} \equiv \text{RM}_{\gamma D_s^+K^-} + M_{K^+K^-\pi^+} - m_{D_s^+}$, with $\text{RM}_{\gamma D_s^+K^-} = \sqrt{(p_{\text{c.m.}} - p_\gamma - p_{D_s^+} - p_{K^-})^2}$, in which $p_{\text{c.m.}}$, p_γ , $p_{D_s^+}$, and p_{K^-} are the four-momenta of the initial e^+e^- system, the radiative photon, D_s^+ , and K^- , respectively. This definition is specified for the $KK\pi$ mode, and a similar definition is applied for the K_S^0K mode. The interval range requirements of $\text{RM}'_{D_s^+K^-}$ in the three sets are presented in Table II. These requirements are based on the Punzi method [50], optimizing the figure of merit (FOM) $\epsilon/(\alpha/2 + \sqrt{B})$, where $\alpha = 3$ indicates the expected

TABLE II. The requirements on the modified recoiling mass $RM'_{\bar{D}^{*0}}$ and on the χ^2 of the 2C kinematic fit for each mode and energy set.

Variables/Sets	I	II	III
$RM'_{\bar{D}^{*0}}$ for $KK\pi$ (MeV/ c^2)	(1999.9, 2034.9)	(1999.9, 2029.9)	(1993.9, 2041.9)
$RM'_{\bar{D}^{*0}}$ for $K_S^0 K$ (MeV/ c^2)	(2001.9, 2021.9)	(1997.9, 2033.9)	(1994.9, 2041.9)
χ^2 in $KK\pi$	< 12.4	< 16.4	< 8.4
χ^2 in $K_S^0 K$	< 20.4	< 23.2	< 12.4

significance, ϵ is the selection efficiency, and B is the number of background events from inclusive MC, as will be discussed in the next section. All possible combinations are retained for later analysis.

IV. BACKGROUND ANALYSIS AND SUPPRESSION

Based on [51], the $e^+e^- \rightarrow D_s^{*+}D_{s1}^-(2536)$, $D_s^{*+} \rightarrow \gamma D_s^+$ events constitute a peaking background and significantly contaminate the signal, since the final state is similar to the signal mode. We require the invariant mass of γD_s^+ ($M_{\gamma D_s^+}$) to satisfy $|M_{\gamma D_s^+} - m_{D_s^{*+}}| > 9 \text{ MeV}/c^2$ to suppress this kind of background, as shown in Fig. 2, where $m_{D_s^{*+}}$ is the nominal mass of D_s^{*+} [43], and the data sample at $\sqrt{s} = 4.682 \text{ GeV}$ is presented as an example. It should be noted that suppressing this peaking background leads to a reduced efficiency at the energy values $\sqrt{s} = 4.661$ and 4.682 , as a result of the relatively larger overlap between the $M_{\gamma D_s^+}$ distributions of the signal and background. After imposing all the above event selection criteria, the distributions of $RM'_{\bar{D}^{*0}}$ are shown in Fig. 3. We generate the exclusive MC samples of $e^+e^- \rightarrow D_s^{*+}D_{s1}^-(2536)$ with $D_s^{*+} \rightarrow \gamma D_s^+$ and $e^+e^- \rightarrow D_s^+D_{s1}^-(2536)$ processes to estimate the background contamination. Their production cross-section line shapes and decay models are taken from the two BESIII measurements [51,52]. The number of

events for $e^+e^- \rightarrow D_s^{*+}D_{s1}^-(2536)$, $D_s^{*+} \rightarrow \gamma D_s^+$ at the 4.682 GeV energy is estimated to be 2.5 in the $KK\pi$ mode and 0.5 in the $K_S^0 K$ mode by simulation. In addition, the backgrounds from $e^+e^- \rightarrow (\gamma_{\text{ISR}})D_s^+D_{s1}^-(2536)$ are determined to be 1.2 events in the $KK\pi$ and 0.3 in the $K_S^0 K$ mode at 4.682 GeV . Therefore, we ignore these two kinds of background in the cross-section measurements, and only consider their impact in the estimation of the systematic uncertainties.

To improve the resolution and further suppress the background, we perform a two-constraint (2C) kinematic fit to all the selected candidates, constraining $M_{K^+\pi^+/\pi^0 K^+}$ to $m_{D_s^+}$ and $RM_{\gamma D_s^+ K^-}$ to $m_{\bar{D}^{*0}}$. Here, $m_{\bar{D}^{*0}}$ is the nominal mass of $\bar{D}^{*0}$ [43]. If there are more than one combination in the event, the candidate with the lowest χ^2 value is chosen. To further suppress the backgrounds, we employed the Punzi method [50] to optimize the χ^2 requirements, as shown in Table II.

V. SIGNAL YIELDS AND CROSS SECTIONS

To extract the number of signal events, we perform an unbinned two-dimensional simultaneous fit to the recoiling-mass distribution of γD_s^+ ($RM_{\gamma D_s^+}$) in the range (2.50, 2.60) GeV/c^2 and of $\gamma(RM_\gamma)$ in the range (4.49, E') GeV/c^2 , where E' represents $\sqrt{s} - 0.025 \text{ GeV}$ (0.025 GeV is the minimum requirement for the photon deposited energy). The line shapes of the $D_{s1}^-(2536)$ and of

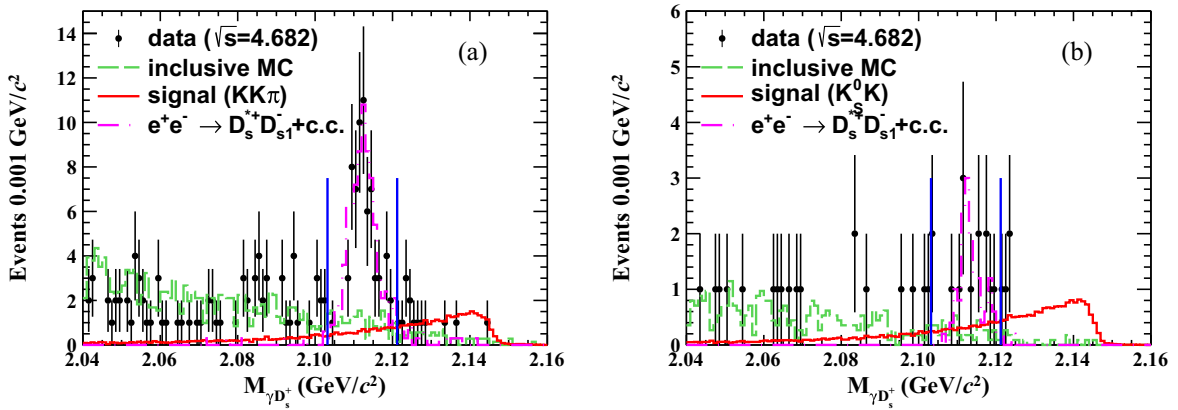


FIG. 2. Distributions of $M_{\gamma D_s^+}$ at $\sqrt{s} = 4.682 \text{ GeV}$ for the $KK\pi$ mode (a) and the $K_S^0 K$ mode (b) after the primary event selection. Dots with error bars indicate data, green dashed lines indicate inclusive MC, red solid lines indicate signal, pink dashed line indicates the peaking background from $e^+e^- \rightarrow D_s^{*+}D_{s1}^-(2536)$, $D_s^{*+} \rightarrow \gamma D_s^+$, and blue solid lines indicate the mass range requirement for $M_{\gamma D_s^+}$.

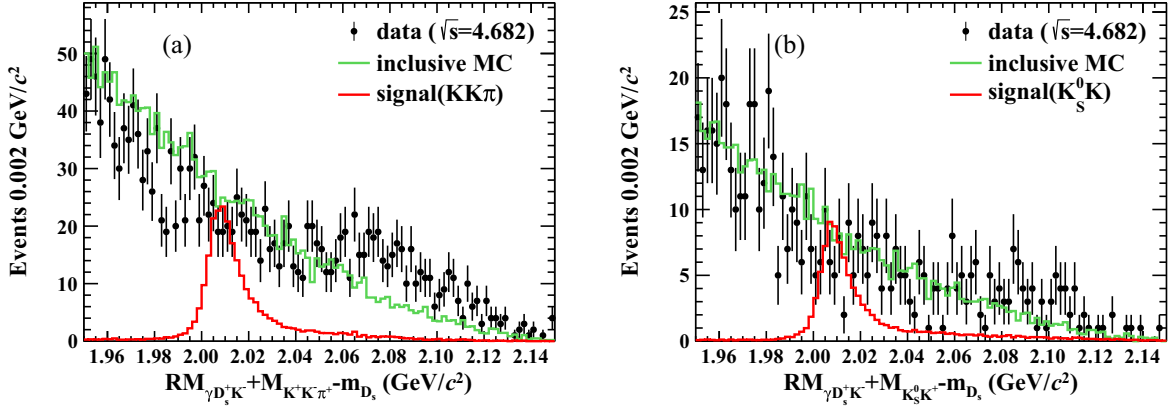


FIG. 3. Distributions of RM'_{D^0} at $\sqrt{s} = 4.682$ GeV for the $KK\pi$ mode (a) and the $K_S^0 K$ mode (b) after the requirement of $M_{\gamma D^+}$. Dots with error bars indicate data, green dashed lines indicate inclusive MC, and red solid lines indicate signal. The number of events in the inclusive MC simulation is normalized to match the data, while the signal is normalized arbitrarily.

the X states are derived from simulated MC shapes using the `RoKeysPdf` method [53] with M_X set to 4.503 GeV/c^2 and Γ_X set to 50 MeV. For the subsequent study of the systematic uncertainties, additional MC samples are generated with Γ_X set to 25, 75, or 100 MeV. The background is described by a second-order Chebychev function for the $RM_{\gamma D^+}$ and a threshold function for the RM_{γ} . This threshold function, derived from the Argus function [54] with interchanged lower and upper boundary parameters, is defined as

$$f_{\text{th}} = \mathcal{N} m \left[1 - \left(\frac{m_0}{m} \right)^2 \right]^p \exp \left[c \left(1 - \left(\frac{m_0}{m} \right)^2 \right) \right], \quad (1)$$

where m is the invariant mass, m_0 is the threshold mass, c and p are shape parameters, and $\mathcal{N}$ is a normalization constant. The signal events in the $KK\pi$ ($N_{KK\pi}$) mode and in the $K_S^0 K$ ($N_{K_S^0 K}$) mode are correlated by

$$N_{K_S^0 K} = f_{\text{sig}} \cdot N_{KK\pi}, \quad (2)$$

$$f_{\text{sig}} = \frac{\epsilon_{K_S^0 K} \cdot \mathcal{B}(D_s^+ \rightarrow K_S^0 K^+) \cdot \mathcal{B}(K_S^0 \rightarrow \pi^+ \pi^-)}{\epsilon_{KK\pi} \cdot \mathcal{B}(D_s^+ \rightarrow K^+ K^- \pi^+)}, \quad (3)$$

where $\epsilon_{K_S^0 K}$ and $\epsilon_{KK\pi}$ are the efficiencies of event selection in the $K_S^0 K$ and $KK\pi$ modes, while $\mathcal{B}(D_s^+ \rightarrow K_S^0 K^+) = (1.450 \pm 0.035)\%$ and $\mathcal{B}(D_s^+ \rightarrow K^+ K^- \pi^+) = (5.37 \pm 0.10)\%$ are the branching fractions for D_s^+ decaying to $K_S^0 K^+$ and $K^+ K^- \pi^+$, respectively; $\mathcal{B}(K_S^0 \rightarrow \pi^+ \pi^-) = (69.20 \pm 0.05)\%$ represents the branching fraction of K_S^0 to $\pi^+ \pi^-$ [43]. Figure 4 shows the fit results with Γ_X set to 50 MeV at $\sqrt{s} = 4.682$ GeV. The obtained signal yields are listed in Table I for each data sample, along with the corresponding statistical significance determined by variations in likelihoods and degrees of freedom with and without the signal.

Since the largest significance of the signal among all c.m. energies is 3.5σ at $\sqrt{s} = 4.682$ GeV, we determine the upper limits of the number of signal events $N_{KK\pi}^{\text{UL}}$ at each energy point. Utilizing the Bayesian method [55], the likelihood distribution $L(x)$ is determined by repeating the fit changing the number of expected signal events. The upper limits at 90% confidence level (CL) are determined by the equation $\int_0^{N_{KK\pi}^{\text{UL}}} L(x) dx / \int_0^\infty L(x) dx = 0.9$. The upper limits of the Born cross section for $e^+ e^- \rightarrow \gamma X$ multiplied by the branching fraction of $X \rightarrow D_s^+ D_{s1}^- (2536)$ are calculated by

$$\sigma^{\text{UL}} \cdot \mathcal{B} = \frac{N_{KK\pi}^{\text{UL}}}{\mathcal{L}_{\text{int}} \cdot (1 + \delta) \cdot \frac{1}{|1 - \Pi|^2} \cdot \epsilon_{KK\pi} \cdot \mathcal{B}_1 \cdot \mathcal{B}_2}, \quad (4)$$

where $\mathcal{L}_{\text{int}}$ is the integrated luminosity at each energy point, $1 + \delta$ is the ISR correction factor based on the QED calculation with 1% accuracy [56] and obtained from the `KKMC` generator, $\frac{1}{|1 - \Pi|^2}$ is the vacuum polarization factor (VP) from Ref. [57], and $\mathcal{B}_1 = (5.37 \pm 0.10)\%$ [43] and $\mathcal{B}_2 = (35.9 \pm 5.9)\%$ [52] are the branching fractions for the $D_s^+ \rightarrow K^+ K^- \pi^+$ and $D_{s1}^- (2536) \rightarrow \bar{D}^{*0} K^-$ decays.

The upper limits of the product of the cross section and branching fraction $\sigma(e^+ e^- \rightarrow \gamma X) \cdot \mathcal{B}(X \rightarrow D_s^+ D_{s1}^- (2536) + \text{c.c.})$ determined at 90% CL, as well as the other input values, are shown in Table I, where only the statistical uncertainty is considered.

VI. SYSTEMATIC UNCERTAINTIES

The sources of systematic uncertainties in the determination of the upper limits of the Born cross-sections $\sigma^{\text{UL}} \cdot \mathcal{B}$ are classified into two categories: the multiplicative terms and the additive terms.

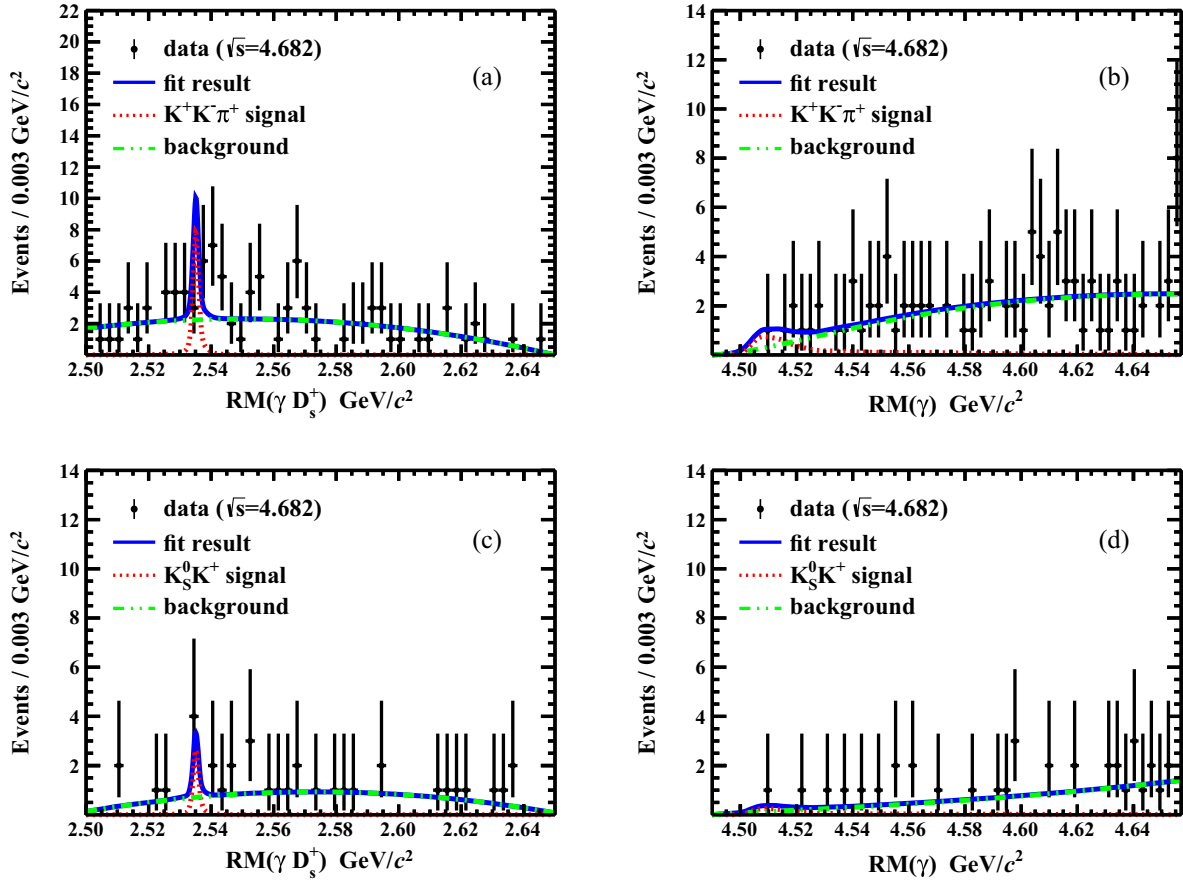


FIG. 4. The results of the two-dimensional simultaneous fit at $\sqrt{s} = 4.682$ GeV, where (a) and (b) are the projected distributions of the γD_s^+ recoiling mass and of the γ recoiling mass for the $KK\pi$ mode, while (c) and (d) are for the $K_S^0 K$ mode. Dots with error bars indicate data, blue solid curves indicate the best fit results, red dashed lines indicate the $D_{s1}^- (2536)$ and X signals, and the green dashed lines indicate the backgrounds.

A. Multiplicative systematic uncertainties

The multiplicative uncertainties include tracking, PID, K_S^0 reconstruction, photon reconstruction, range requirements for $M_{K^+\pi^-}$, $M_{K^+K^-}$, $M_{\pi^+\pi^-}$, $M_{K^+K^-\pi^+}/K_S^0 K^+$, and $\text{RM}_{\gamma D_s^+ K^-}$, VP factor, luminosity, branching fractions of intermediate states, physical model, kinematic fit, and $(1 + \delta) \cdot \epsilon_{KK\pi}$.

The systematic uncertainty for tracking is assigned to be 1.0% for each π/K track [58], while the uncertainty for PID is assigned to be 1.0% [58].

We quote 2.0% as the systematic uncertainty caused by K_S^0 reconstruction, based on Ref. [58], in which the same K_S^0 reconstruction method is applied.

The uncertainty due to photon detection efficiency is determined to be 1.0% per photon [51], according to a study using as control sample $J/\psi \rightarrow \rho\pi$ events.

The systematic uncertainties due to the range requirements on $M_{K^+\pi^-}$, $M_{K^+K^-}$, and $M_{K^+K^-\pi^+}$ for the $KK\pi$ mode, and on $M_{\pi^+\pi^-}$ and $M_{K_S^0 K^+}$ for the $K_S^0 K$ mode, stem from the resolution difference between data and MC and are determined by comparing the signal shapes of data and MC; they are found to be 1.2%, $< 0.1\%$ (negligible),

0.2%, 0.3%, and 0.6%, respectively. Since a simultaneous fit is performed in this analysis, only the uncertainties associated with $M_{K^+\pi^-}$, $M_{K^+K^-}$, and $M_{K^+K^-\pi^+}$ contribute to the global multiplicative uncertainty, even though all of them affect the correlation coefficient f_{sig} . Since no significant signal is observed in the recoil mass of $\gamma D_s^+ K^-$ in data, a different method is employed to study the systematic uncertainty from the $\text{RM}_{\gamma D_s^+ K^-}$ mass window requirement; we smear the γ energy distribution by a Gaussian with 1% uncertainty and reconstruct the smeared recoil mass $\text{RM}_{\gamma D_s^+ K^-}^{\text{smear}}$. The difference in efficiency by applying the same requirement in the $\text{RM}_{\gamma D_s^+ K^-}$ and $\text{RM}_{\gamma D_s^+ K^-}^{\text{smear}}$ distributions is taken as the related systematic uncertainty. We assign 0.7% and 0.2% for the range requirement of $\text{RM}_{\gamma D_s^+ K^-}$ in the $KK\pi$ mode and the $K_S^0 K$ mode, respectively.

The uncertainty from the vacuum polarization factor is less than 0.1% [57].

The integrated luminosity is measured using Bhabha events, with an uncertainty of about 1.0% at each energy point [35].

TABLE III. The multiplicative systematic uncertainties associated with $KK\pi$ mode, expressed as percentages.

$\sqrt{s}$ (GeV)	4.612	4.628	4.641	4.661	4.682	4.699	4.74	4.75	4.781	4.843	4.918	4.951
Tracking	4.0	4.0	4.0	4.0	4.0	4.0	4.0	4.0	4.0	4.0	4.0	4.0
PID	4.0	4.0	4.0	4.0	4.0	4.0	4.0	4.0	4.0	4.0	4.0	4.0
γ reconstruction	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
$M_{K^+\pi^-}$ range	1.2	1.2	1.2	1.2	1.2	1.2	1.2	1.2	1.2	1.2	1.2	1.2
$M_{K^+K^-\pi^+}$ range	0.2	0.2	0.2	0.2	0.2	0.2	0.2	0.2	0.2	0.2	0.2	0.2
$\text{RM}_{\gamma D_s^+ K^-}$ range	0.7	0.7	0.7	0.7	0.7	0.7	0.7	0.7	0.7	0.7	0.7	0.7
VP	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1
Luminosity	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
$\mathcal{B}(D_s^+ \rightarrow K^+ K^- \pi^+)$	1.9	1.9	1.9	1.9	1.9	1.9	1.9	1.9	1.9	1.9	1.9	1.9
$\mathcal{B}(D_{s1}^-(2536) \rightarrow \bar{D}^{*0} K^-)$	16.4	16.4	16.4	16.4	16.4	16.4	16.4	16.4	16.4	16.4	16.4	16.4
Physical model	3.6	3.6	3.6	3.6	3.6	3.6	3.6	3.6	3.6	3.6	3.6	3.6
Kinematic fit	5.8	6.2	8.1	4.7	5.5	3.4	3.0	3.1	3.1	7.6	6.7	6.9
$(1 + \delta) \cdot \epsilon_{KK\pi}$	0.5	0.4	0.8	3.0	3.3	5.5	4.8	6.0	6.9	4.3	4.2	4.9
Total	18.8	19.0	19.7	18.8	19.0	19.1	18.8	19.2	19.5	19.9	19.6	19.8

The systematic uncertainties associated with the branching fractions $\mathcal{B}(D_s^+ \rightarrow K^+ K^- \pi^+)$, $\mathcal{B}(D_s^+ \rightarrow K_S^0 K^+)$, $\mathcal{B}(K_S^0 \rightarrow \pi^+ \pi^-)$, and $\mathcal{B}(D_{s1}^-(2536) \rightarrow \bar{D}^{*0} K^-)$ are quoted as 1.9% [43], 2.4% [43], 0.1% [43], and 16.4% [52], respectively.

The uncertainty associated with the physical model of the $e^+e^- \rightarrow \gamma X$ process is estimated by changing the PHSP to a helicity amplitude (HELAMP) model [42] when generating the signal MC sample. The differences in efficiency between the PHSP and the HELAMP model, 3.6% for the $KK\pi$ mode and 3.1% for the $K_S^0 K$ mode, are considered as systematic uncertainties. The PHSP model, which results with a lower efficiency, is adopted as the nominal model for a conservative measurement.

To study the systematic uncertainty caused by the kinematic fit, we correct the helix parameters of charged tracks in the MC simulation [59]. The efficiency difference with and without the helix correction, as shown in Table III, is taken as the systematic uncertainty.

In the nominal results, the detection efficiencies and ISR corrections $(1 + \delta) \cdot \epsilon_{KK\pi}$ are obtained from the MC sample, with the cross-section line shape described by E_γ^3/s . The uncertainty from the input cross-section line shape is estimated by using the relativistic Breit-Wigner function of the $Y(4660)$ state instead. The changes in the resultant Born cross sections, shown in Table III, are taken as the systematic uncertainty from the $(1 + \delta) \cdot \epsilon_{KK\pi}$ term. Differing ISR effects below, on, and above the resonance peak lead to distinct systematic uncertainties related to this issue.

Based on Eq. (4), all the multiplicative systematic uncertainties associated with the $KK\pi$ mode for each energy point are listed in Table III, and the total systematic uncertainties are obtained by adding them in quadrature assuming no correlation among all the sources. To take into account the multiplicative systematic uncertainties in the upper limit calculation, the normalized likelihood

distributions are smeared with a Gaussian function with a mean of $\epsilon_{KK\pi}$ and a standard deviation of $\delta_e^{\text{abs}} = \epsilon_{KK\pi} \cdot \delta_e^{\text{rel}}$, where δ_e^{abs} and δ_e^{rel} are the absolute and relative multiplicative systematic uncertainties, respectively. The smeared likelihood is defined as

$$\mathcal{L}(N_{KK\pi}) = \int_0^1 \mathcal{L}'\left(\frac{\epsilon}{\epsilon_{KK\pi}} N_{KK\pi}\right) \frac{1}{\sqrt{2\pi}\delta_e^{\text{abs}}} e^{-\frac{(\epsilon - \epsilon_{KK\pi})^2}{2\delta_e^{\text{abs}2}}} d\epsilon. \quad (5)$$

B. Additive systematic uncertainties

The additive systematic uncertainties arise from the fit process and mainly include the uncertainties associated with the background shape and the correlation coefficient f_{sig} , which is related to the efficiency ratio $\epsilon_{K_S^0 K}/\epsilon_{KK\pi}$, as well as the branching fractions $\mathcal{B}(D_s^+ \rightarrow K_S^0 K^+)$, $\mathcal{B}(K_S^0 \rightarrow \pi^+ \pi^-)$, and $\mathcal{B}(D_s^+ \rightarrow K^+ K^- \pi^+)$.

We estimate the systematic uncertainty from background shape by using a first-order Chebyshev function instead of the second-order Chebyshev function in the $\text{RM}_{\gamma D_s^+}$ projection, and a second-order Chebyshev function instead of the threshold function in the RM_γ projection to describe the background shapes. The highest upper limit of the variations in the background shapes is assigned as the associated systematic uncertainty.

We account for the systematic uncertainty arising from the efficiency ratio $\epsilon_{K_S^0 K}/\epsilon_{KK\pi}$ and the branching fractions $\mathcal{B}(D_s^+ \rightarrow K_S^0 K^+)$, $\mathcal{B}(K_S^0 \rightarrow \pi^+ \pi^-)$, and $\mathcal{B}(D_s^+ \rightarrow K^+ K^- \pi^+)$ in the simultaneous fit, employing the same method as the multiplicative systematic uncertainties in Sec. VIA. Note that the uncertainties associated with tracking and PID, which contribute to the efficiency ratio $\epsilon_{K_S^0 K}/\epsilon_{KK\pi}$, are partially correlated; therefore, their effects are partially canceled. The uncertainties related to the γ reconstruction are fully canceled out. Other uncertainty

TABLE IV. The uncertainties of the correlation coefficient $\Delta(f_{\text{sig}})$ evaluated at each energy point, expressed as percentages.

$\sqrt{s}$ (GeV)	4.612	4.628	4.641	4.661	4.682	4.699	4.740	4.750	4.781	4.843	4.918	4.951
Tracking	2.0	2.0	2.0	2.0	2.0	2.0	2.0	2.0	2.0	2.0	2.0	2.0
PID	2.0	2.0	2.0	2.0	2.0	2.0	2.0	2.0	2.0	2.0	2.0	2.0
K_S^0 reconstruction	2.0	2.0	2.0	2.0	2.0	2.0	2.0	2.0	2.0	2.0	2.0	2.0
Physical model	4.8	4.8	4.8	4.8	4.8	4.8	4.8	4.8	4.8	4.8	4.8	4.8
$M_{K^+\pi^-}$ range	1.2	1.2	1.2	1.2	1.2	1.2	1.2	1.2	1.2	1.2	1.2	1.2
$M_{\pi^+\pi^-}$ range	0.3	0.3	0.3	0.3	0.3	0.3	0.3	0.3	0.3	0.3	0.3	0.3
$M_{K^+K^-\pi^+}/K_S^0K^+$ range	0.6	0.6	0.6	0.6	0.6	0.6	0.6	0.6	0.6	0.6	0.6	0.6
$\text{RM}_{\gamma D_s^+ K^-}$ range	0.7	0.7	0.7	0.7	0.7	0.7	0.7	0.7	0.7	0.7	0.7	0.7
Kinematic fit	5.5	5.8	7.6	4.7	5.2	3.3	2.9	3.1	3.0	8.4	8.2	6.5
$\mathcal{B}(D_s^+ \rightarrow K_S^0 K^+)$	2.4	2.4	2.4	2.4	2.4	2.4	2.4	2.4	2.4	2.4	2.4	2.4
$\mathcal{B}(K_S^0 \rightarrow \pi^+\pi^-)$	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1	0.1
$\mathcal{B}(D_s^+ \rightarrow K^+ K^- \pi^+)$	1.9	1.9	1.9	1.9	1.9	1.9	1.9	1.9	1.9	1.9	1.9	1.9
Total	8.8	9.0	10.2	8.3	8.6	7.6	7.5	7.5	7.5	10.8	10.7	9.5

TABLE V. The results of $\sigma(e^+e^- \rightarrow \gamma X) \cdot \mathcal{B}(X \rightarrow D_s^+ D_{s1}^- (2536) + \text{c.c.})$ under different assumptions of X 's width ($\Gamma_X = 25, 50, 75, 100$ MeV) including the systematic uncertainties. The $N_{KK\pi}^{\text{UL}}$ and $\sigma_{\text{sys}}^{\text{UL}} \cdot \mathcal{B}$ values represent the upper limits of the number of signal events and of the product of the cross section and branching fraction at 90% CL. The contributions of $K_S^0 K$ mode have been included via correlated branching fractions and efficiencies.

Γ_X	25 MeV		50 MeV		75 MeV		100 MeV	
$\sqrt{s}$ (GeV)	$N_{KK\pi}^{\text{UL}}$	$\sigma_{\text{sys}}^{\text{UL}} \cdot \mathcal{B}$ (pb)	$N_{KK\pi}^{\text{UL}}$	$\sigma_{\text{sys}}^{\text{UL}} \cdot \mathcal{B}$ (pb)	$N_{KK\pi}^{\text{UL}}$	$\sigma_{\text{sys}}^{\text{UL}} \cdot \mathcal{B}$ (pb)	$N_{KK\pi}^{\text{UL}}$	$\sigma_{\text{sys}}^{\text{UL}} \cdot \mathcal{B}$ (pb)
4.612	1.7	26.9	1.7	26.9	1.7	26.9	1.7	26.9
4.628	2.8	8.6	2.8	8.6	3.1	9.5	3.1	9.5
4.641	4.3	12.8	5.5	16.3	5.9	17.5	5.8	17.2
4.661	2.7	12.7	2.8	13.1	3.3	15.4	3.2	15.0
4.682	10.2	10.7	13.1	13.8	14.7	15.5	15.4	16.2
4.699	4.8	12.9	5.7	15.3	6.3	16.9	6.7	18.0
4.740	1.8	14.2	1.9	15.0	1.9	15.0	1.9	15.0
4.750	3.4	12.0	4.4	15.4	4.7	16.5	4.8	16.8
4.781	1.9	4.6	2.1	5.1	2.4	5.8	2.5	6.1
4.843	1.8	4.6	1.8	4.6	1.9	4.8	2.0	5.1
4.918	5.2	30.6	5.3	31.1	6.8	39.9	7.0	41.0
4.951	1.7	13.5	1.7	13.5	1.7	13.5	1.7	13.5

sources of the efficiency ratio $\epsilon_{K_S^0 K}/\epsilon_{KK\pi}$ associated with the physical model, mass interval requirement, and kinematic fit are considered as independent in the two modes. All the uncertainties from different sources are treated as independent, and the total systematic uncertainty of f_{sig} is obtained by summing them in quadrature. The systematic uncertainties from f_{sig} at each energy point are presented in Table IV. We incorporate the f_{sig} and its related uncertainty at each energy point in the simultaneous fit, adopting the highest upper limit as the value considering the associated systematic uncertainty.

After considering the systematic uncertainties, Table V and Fig. 5 represent the upper limits of the product of the cross section and the branching fraction $\sigma(e^+e^- \rightarrow \gamma X) \cdot \mathcal{B}(X \rightarrow D_s^+ D_{s1}^- (2536))$, assuming Γ_X is 25, 50, 75, or 100 MeV.

VII. SUMMARY

Based on e^+e^- collision data at c.m. energies from 4.612 to 4.951 GeV collected by the BESIII spectrometer, corresponding to an integrated luminosity of 5.8fb^{-1} , the exotic molecular state X ($J^{PC} = 1^{-+}$) is searched for the first time via the process $e^+e^- \rightarrow \gamma X, X \rightarrow D_s^+ D_{s1}^- (2536)$. No significant signal is observed, and the upper limits of $\sigma(e^+e^- \rightarrow \gamma X) \cdot \mathcal{B}(X \rightarrow D_s^+ D_{s1}^- (2536))$ are determined at 90% CL, assuming $M_X = 4.503 \text{ GeV}/c^2$ and $\Gamma_X = 25, 50, 75$, or 100 MeV. The obtained upper limits are shown in Table V and Fig. 5. These upper limits range from 5 to 45 pb, while typically 15 pb around 4.68 GeV. Assuming the total cross section of $e^+e^- \rightarrow Y(4660)$ is about 300 pb [43] and the branching fraction of $Y(4660) \rightarrow \gamma X$ being 0.1% [same to $\mathcal{B}(Y(4260) \rightarrow \gamma X')$ estimated in Ref. [34],

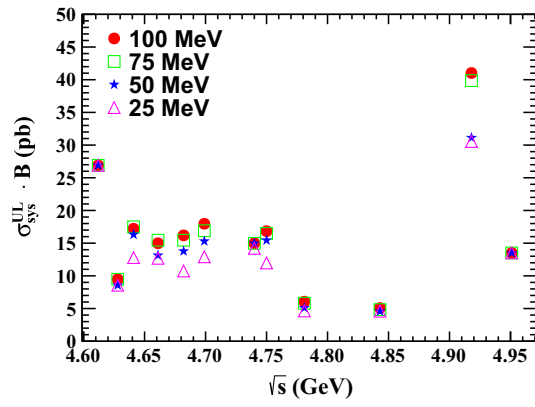


FIG. 5. The upper limits of the product of the cross section and branching fraction $\sigma(e^+e^- \rightarrow \gamma X) \cdot B(X \rightarrow D_s^+ D_{s1}^-(2536) + \text{c.c.})$ at each energy points assuming the width $\Gamma_X = 25, 50, 75$, or 100 MeV at 90% CL.

where X' decays into nonstrange D meson pairs], the product of the cross section and the branching fraction is 0.3 pb, which is 50 times lower than the upper limit determined in this analysis. At $\sqrt{s} = 4.682$ GeV, there is evidence of a signal with 3.5σ significance when $\Gamma_X = 50$ MeV. However, this evidence may only be a local and statistical fluctuation. Therefore, more experimental data are needed to confirm or exclude it by considering the global significance and the systematic uncertainties.

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DATA AVAILABILITY

The data supporting this study's findings are available within the article.

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